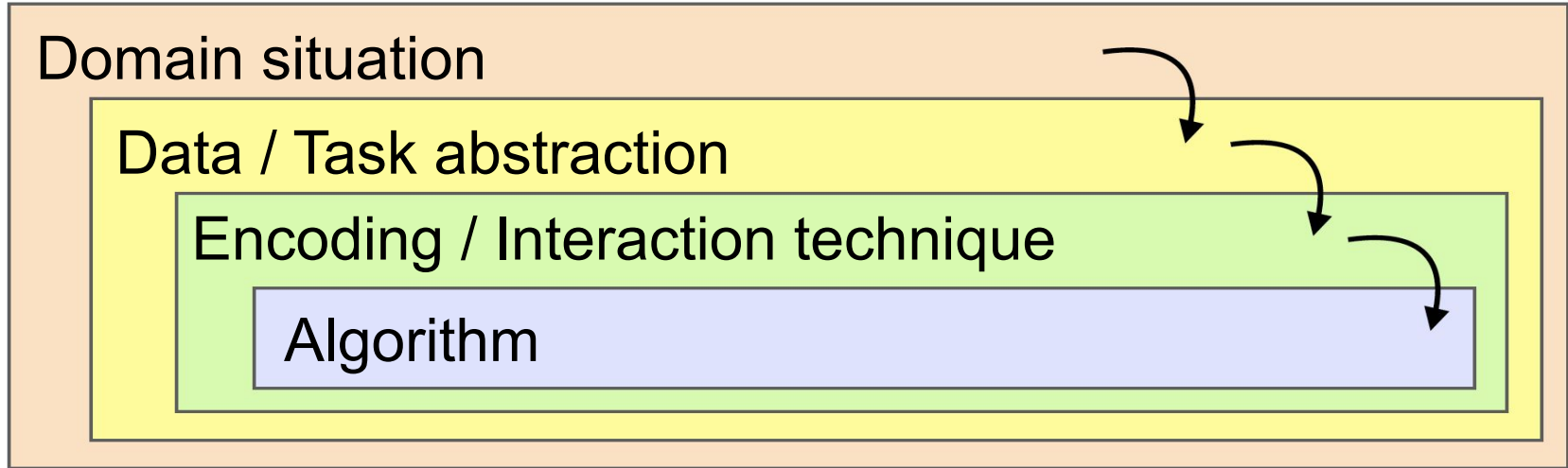


Visualizing Multi-Dimensional Data

Chen He

Data abstraction: Multi-dimensional data

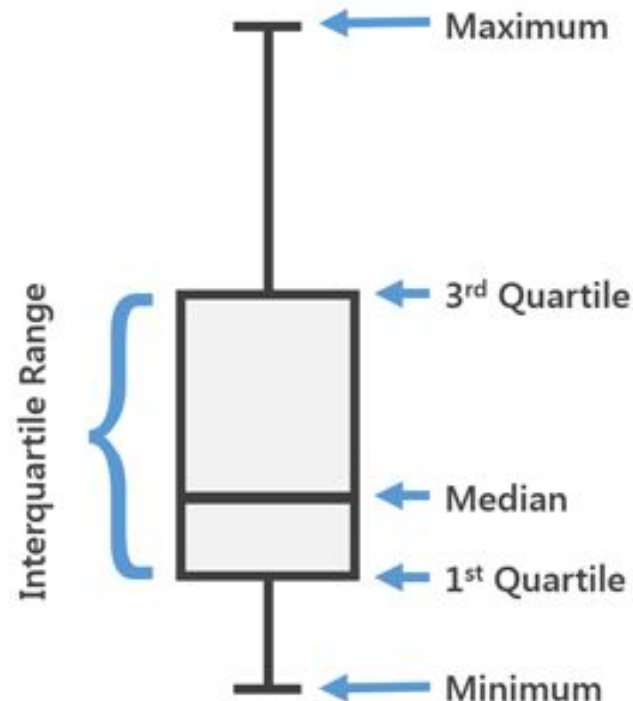


1-dimensional data -- Box plot

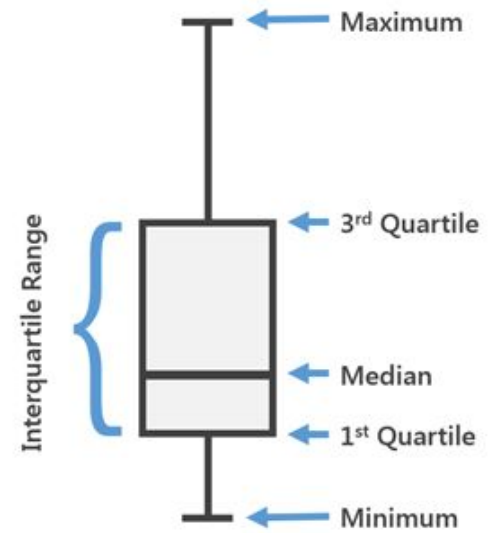
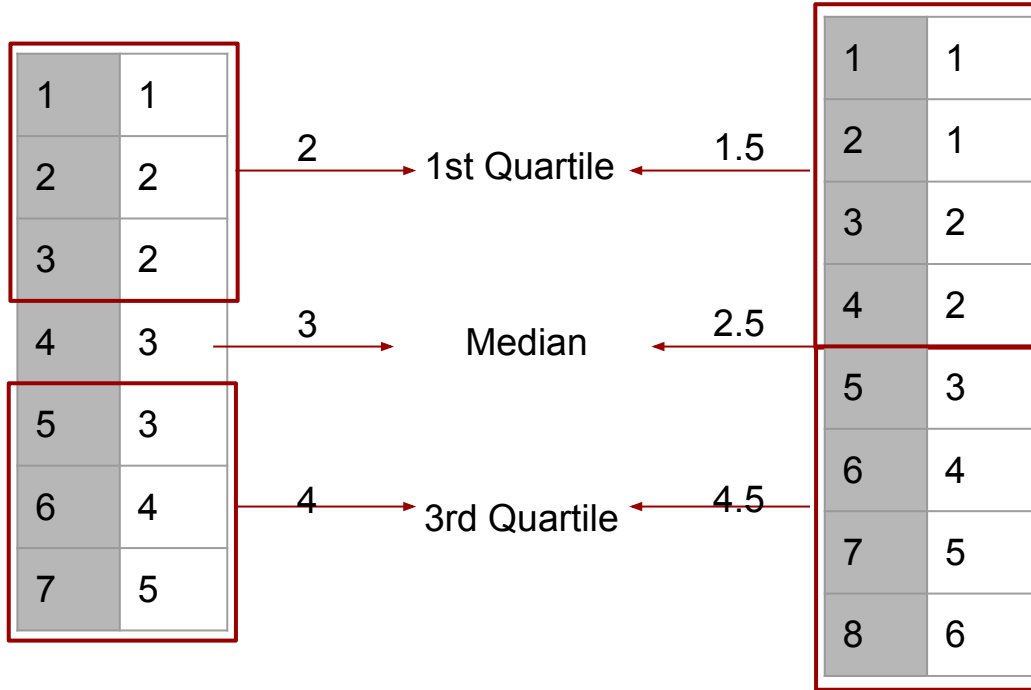
Use quartiles to graphically depict a group of numerical data.

Pros Summarization;
 Easy comparison between datasets.

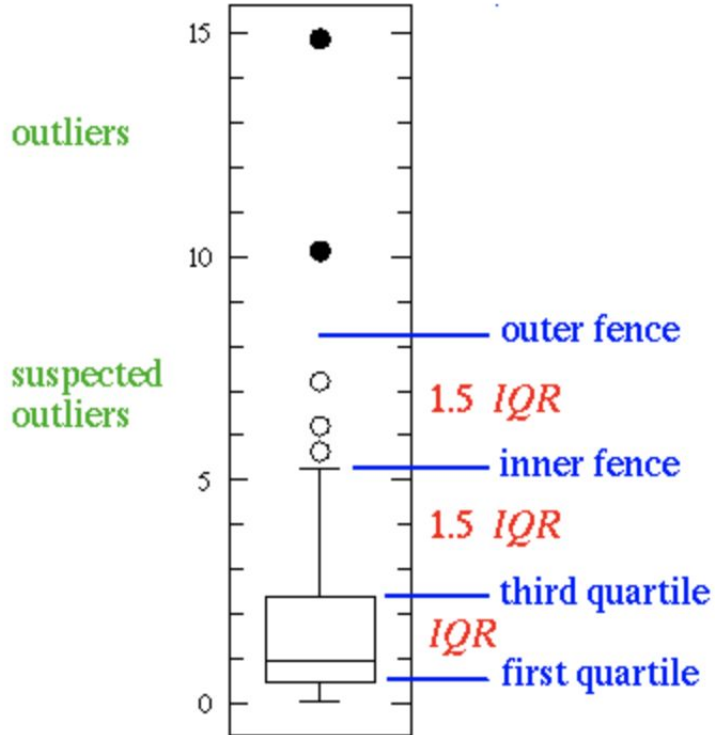
Cons Details are invisible;



1-dimensional data -- Box plot



1-dimensional data -- Box plot



IQR: interquartile range

Suspected outliers:

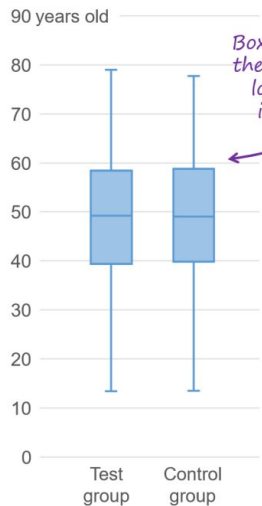
$> 1.5 \text{ IQR} + 3\text{rd Quartile};$
 $< 1\text{st Quartile} - 1.5 \text{ IQR}.$

Outliers:

$> 3 \text{ IQR} + 3\text{rd Quartile};$
 $< 1\text{st Quartile} - 3 \text{ IQR}.$

“I’ve stopped using box plots.”

Study Participants by Age

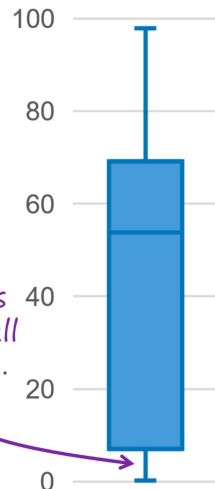


Box plots make the two groups look almost identical...

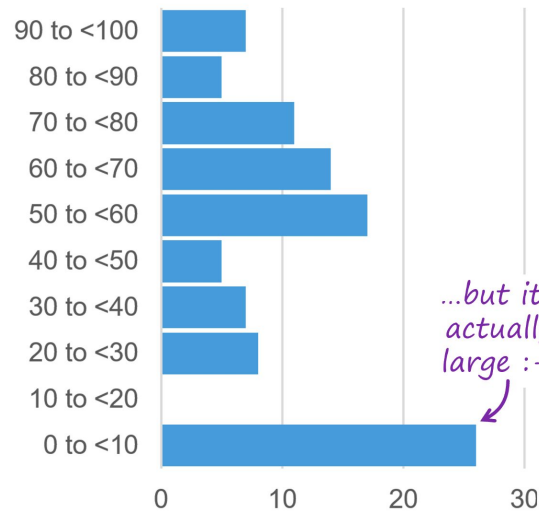
Study Participants by Age



...but they definitely aren't :-)



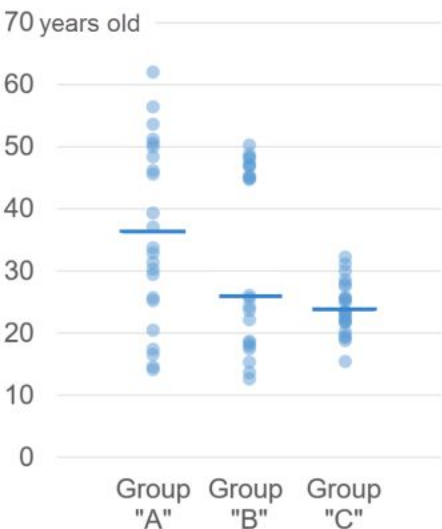
This looks like a small quantity...



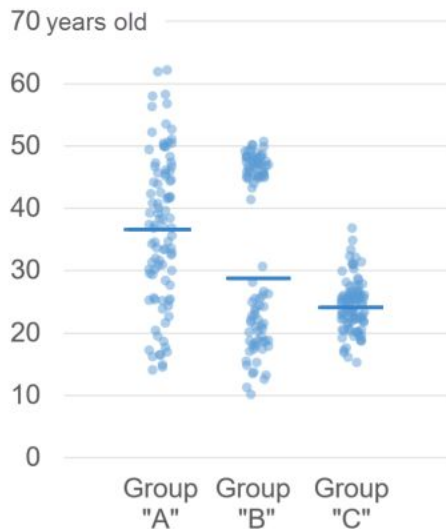
...but it's actually large :-)

“I’ve stopped using box plots.”

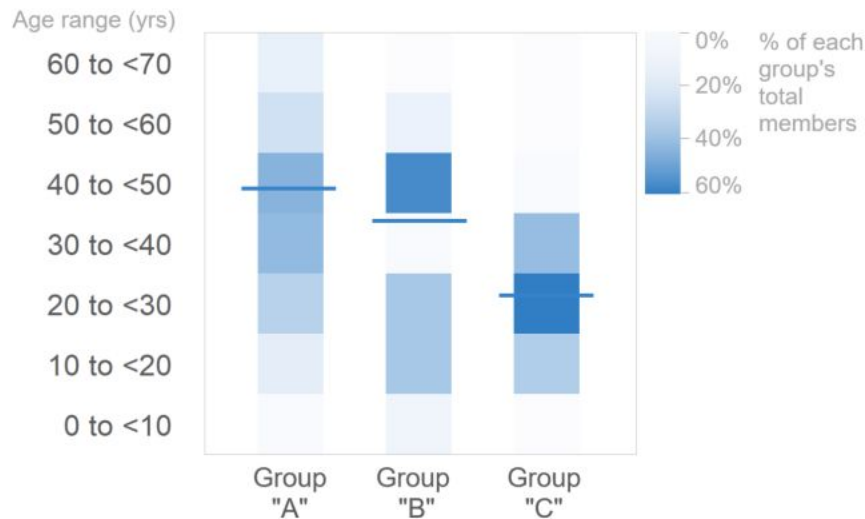
Age Distribution by Group



Age Distribution by Group



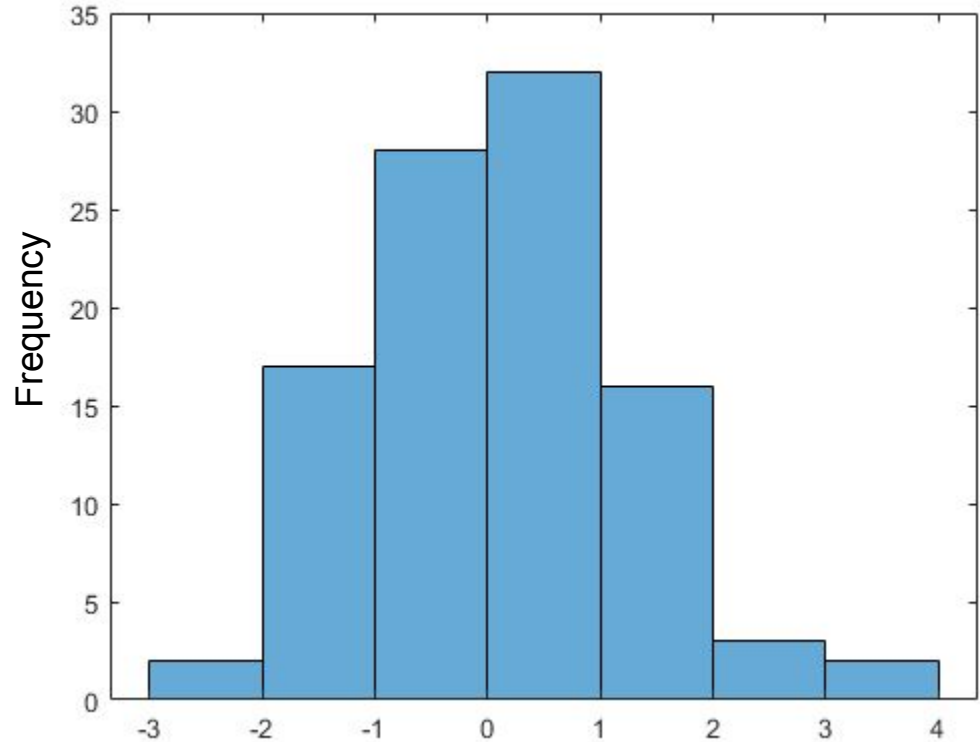
Age Distribution by Group



1-dimensional data -- Histogram

Depict the frequency distribution of a univariate data set.

By convention, an interval =
[lower bound, upper bound)

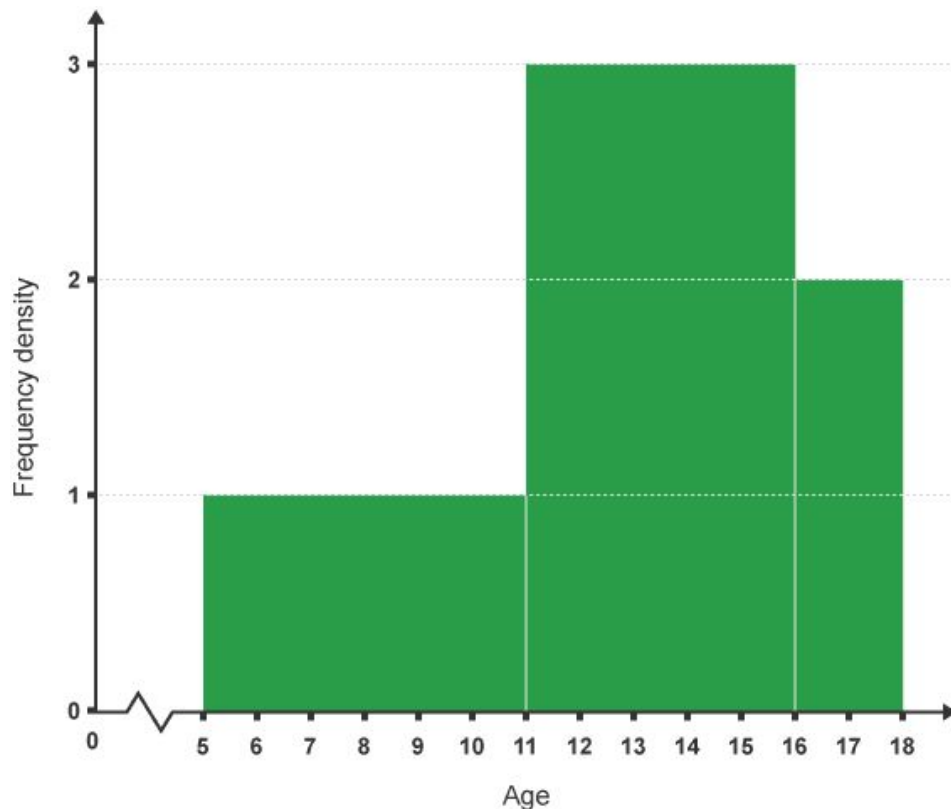


1-dimensional data -- Histogram

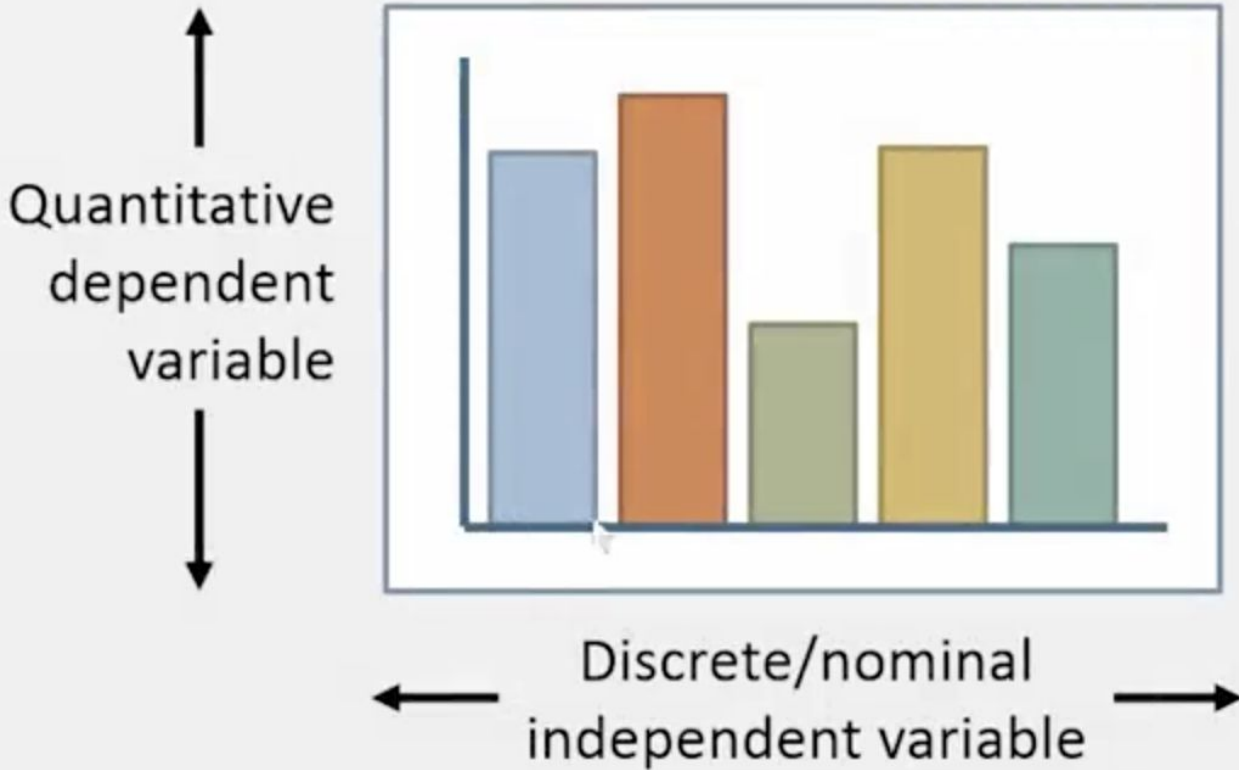
Unequal bin sizes (not recommended)

Frequency (the area) =
Class Width x Frequency Density.

Density is not easy to understand.



2-dimensional data -- Bar chart

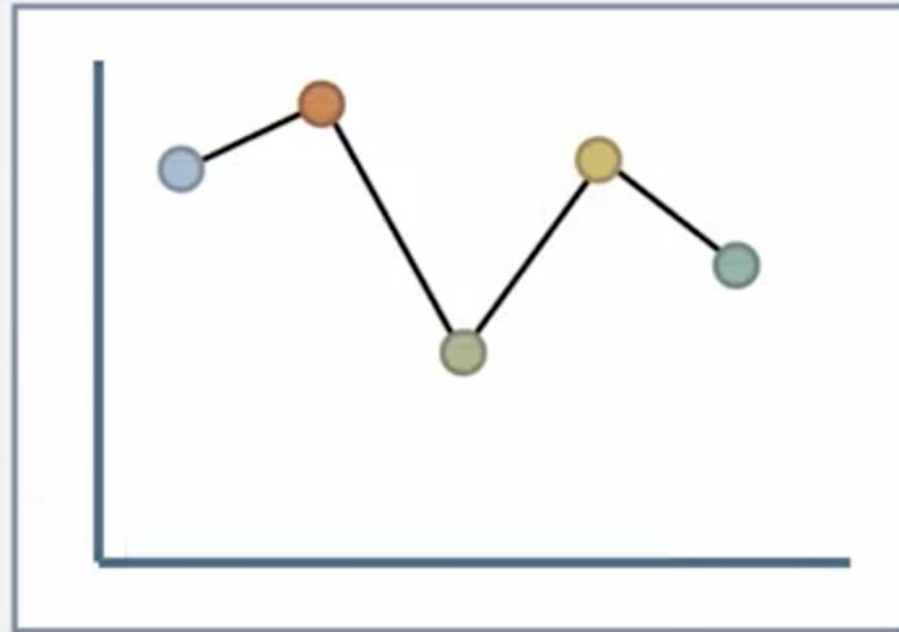


Benefits from both position (top of bar) and length (size of bar)

Quantitative		Ordinal		Nominal	
Position	••	Position	••	Position	••
Length	==	Density	•••	Hue	•••
Angle	∠	Saturation	•••	Density	•••
Slope	/	Hue	•••	Saturation	•••
Area	••	Length	==	Shape	••
Density	•••	Angle	∠	Length	==
Saturation	•••	Slope	/	Angle	∠
Hue	•••	Area	••	Slope	/
Shape	••	Shape	••	Area	••

2-dimensional data -- Line chart

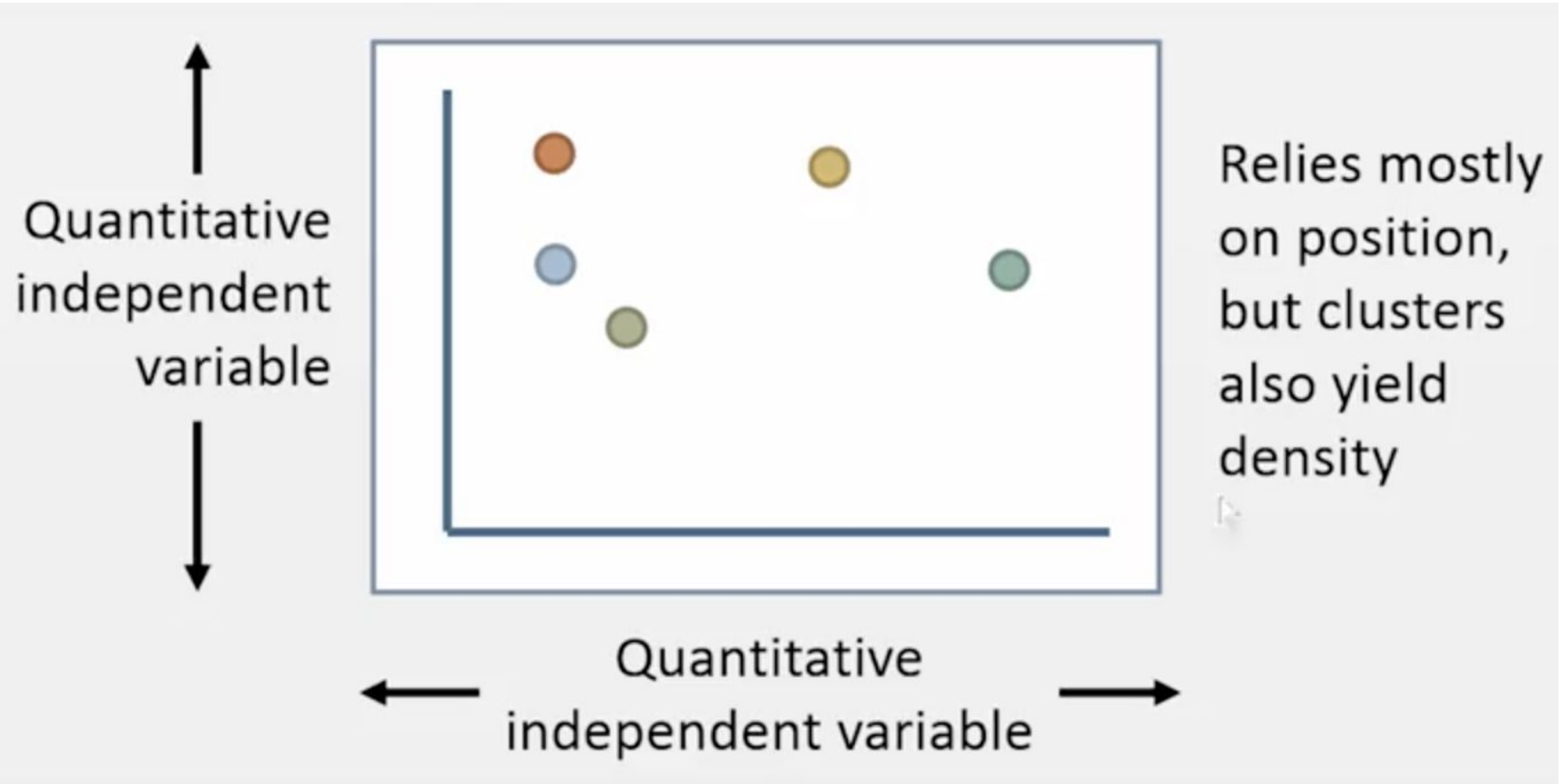
↑
Quantitative
continuous
dependent
variable



Benefits from
position but
not length

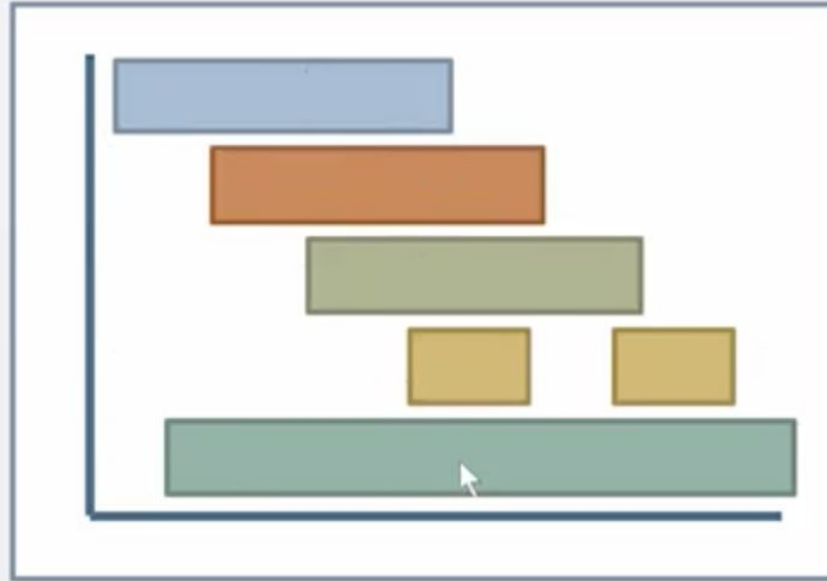
← Quantitative continuous
independent variable →

2-dimensional data -- Scatter plot



2-dimensional data -- Gantt chart

Discrete/nominal
independent
variable



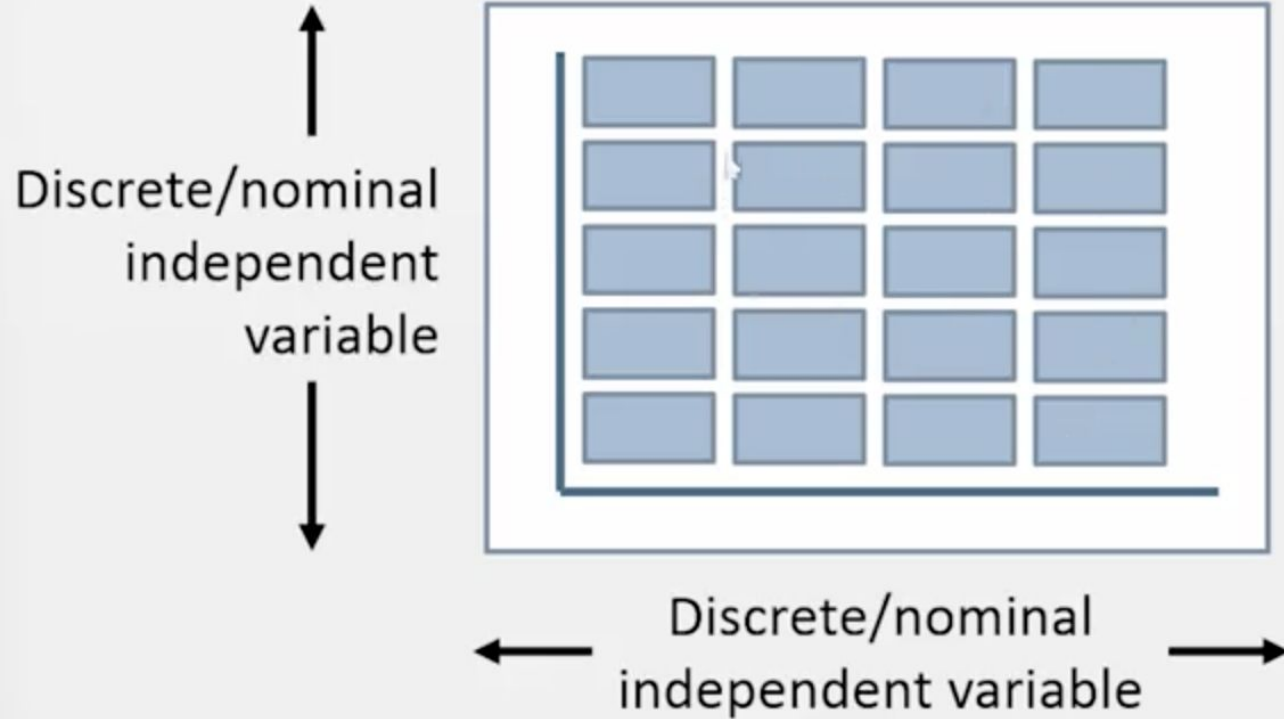
Benefits from
both position
and length

Quantitative
independent variable

2-dimensional data -- Gantt chart



2-dimensional data -- Table



Benefits from
position only

(notice the lateral
inhibition flashing?)



2-dimensional data -- What chart to use?

Dep.	Quantitative Continuous	Bar	Line
	Quantitative Discrete	Bar	Bar
Ind.	Quantitative Continuous	Gantt	Scatter
	Nominal or Q. Discrete	Table	Gantt
		Nominal or Q. Discrete	Quantitative Continuous
Independent			

How about this chart?



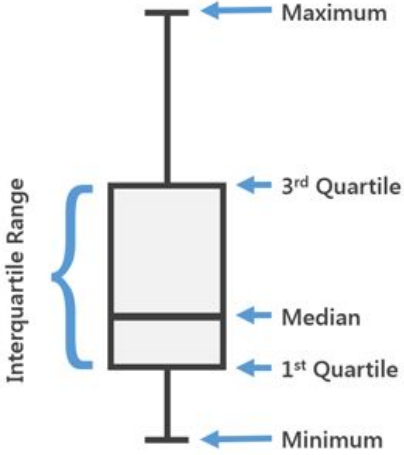
Figure 2. Doctoral candidates' research writing profiles

So far - 1D data

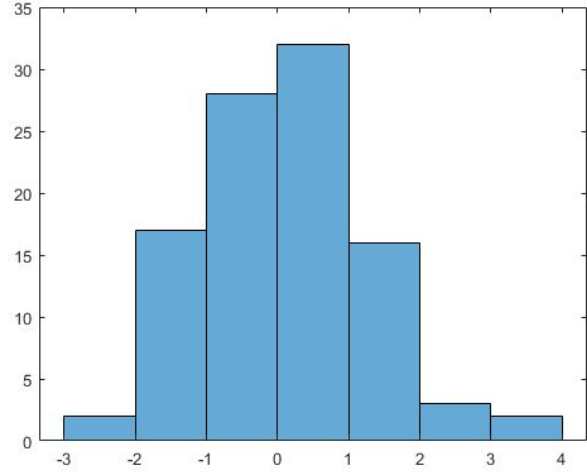
word clouds



box plot



histogram

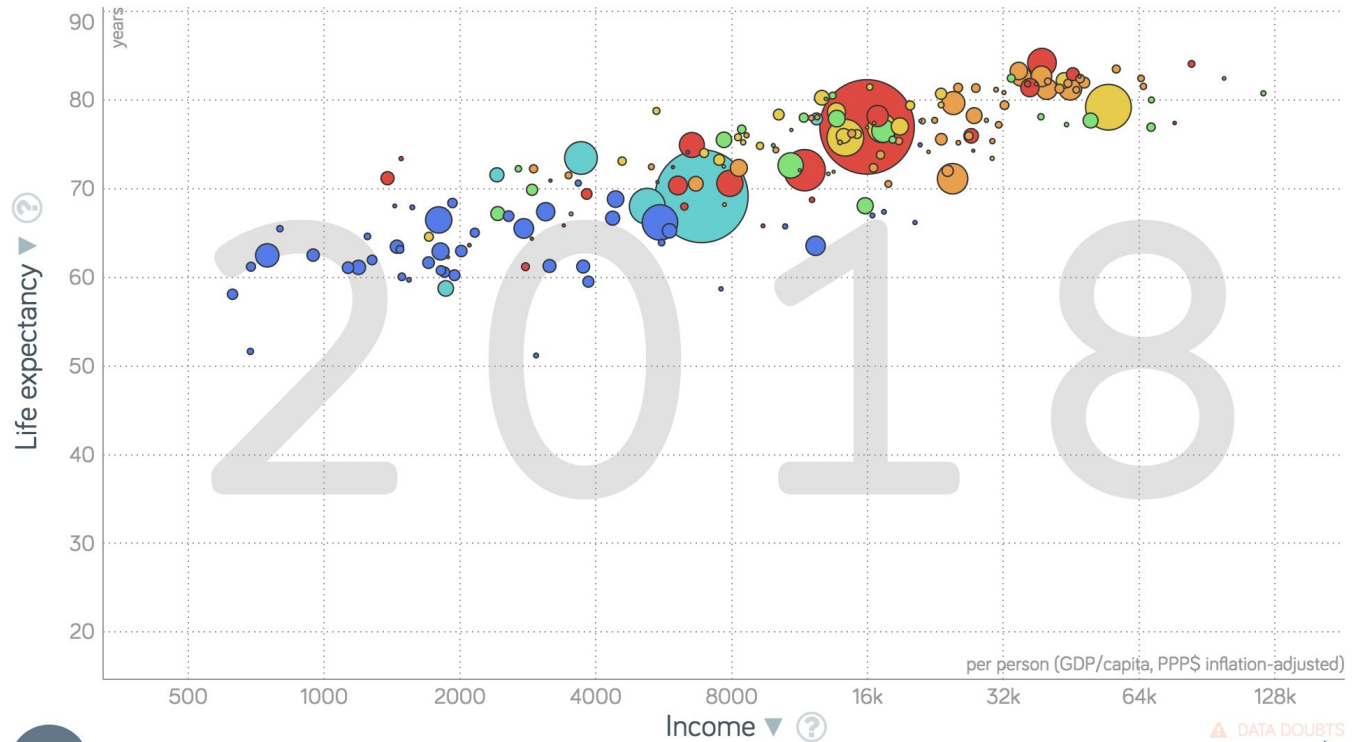


So far - 2D data

Bar chart, scatter plot, line chart, gantt chart, and table.

Dep.	Quantitative Continuous	Bar	Line
	Quantitative Discrete	Bar	Bar
Ind.	Quantitative Continuous	Gantt	Scatter
	Nominal or Q. Discrete	Table	Gantt
		Nominal or Q. Discrete	Quantitative Continuous
Independent			

Multi-dimensional data -- Add additional dimensions on top of 2D charts



Quantitative	Ordinal	Nominal			
Position	●●	Position	●●	Position	●●
Length	==	Density	●●●	Hue	●●●
Angle	∠	Saturation	●●●	Density	●●●
Slope	∕	Hue	●●●	Saturation	●●●
Area	●●	Length	==	Shape	●▲■
Density	●●●	Angle	∠	Length	==
Saturation	●●●	Slope	∕	Angle	∠
Hue	●●●	Area	●●	Slope	∕
Shape	●▲■	Shape	●▲■	Area	●●

Color



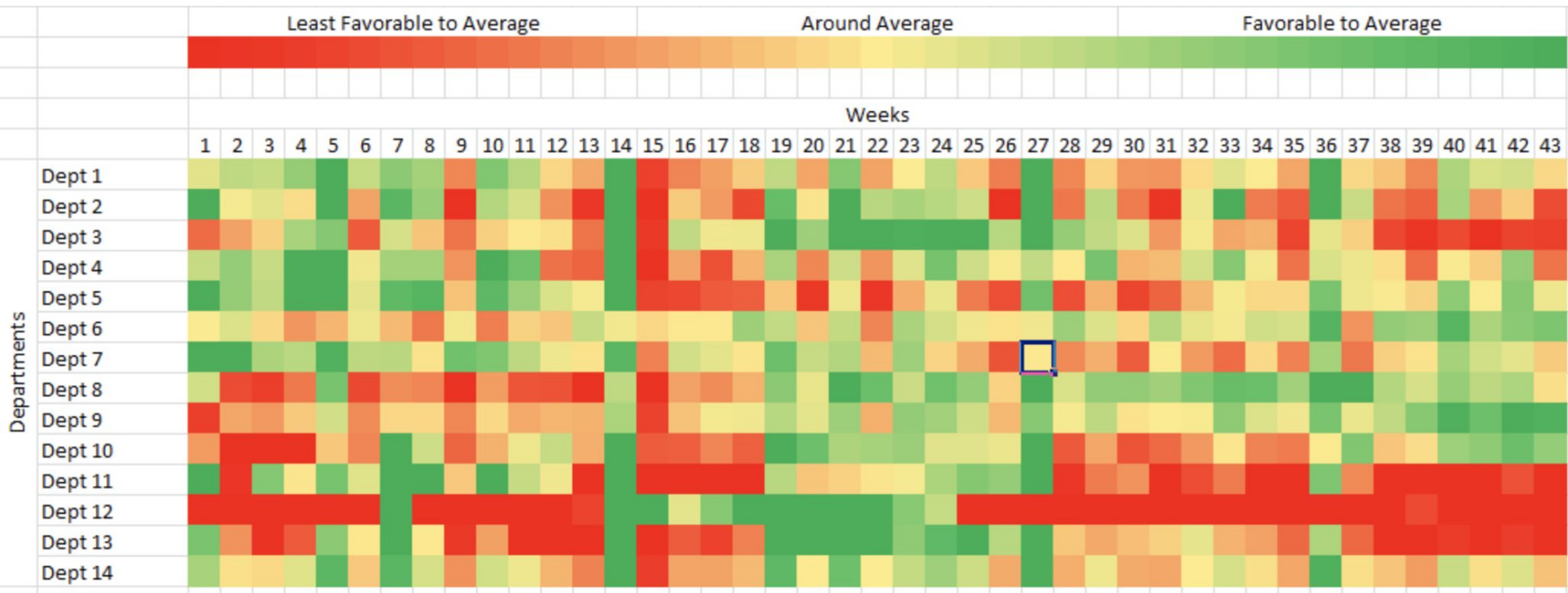
Select

- Afghanistan
- Albania
- Algeria
- Andorra
- Angola
- Antigua and Barbuda
- ...

Size

Zoom

Multi-dimensional data -- Add additional dimensions on top of 2D charts

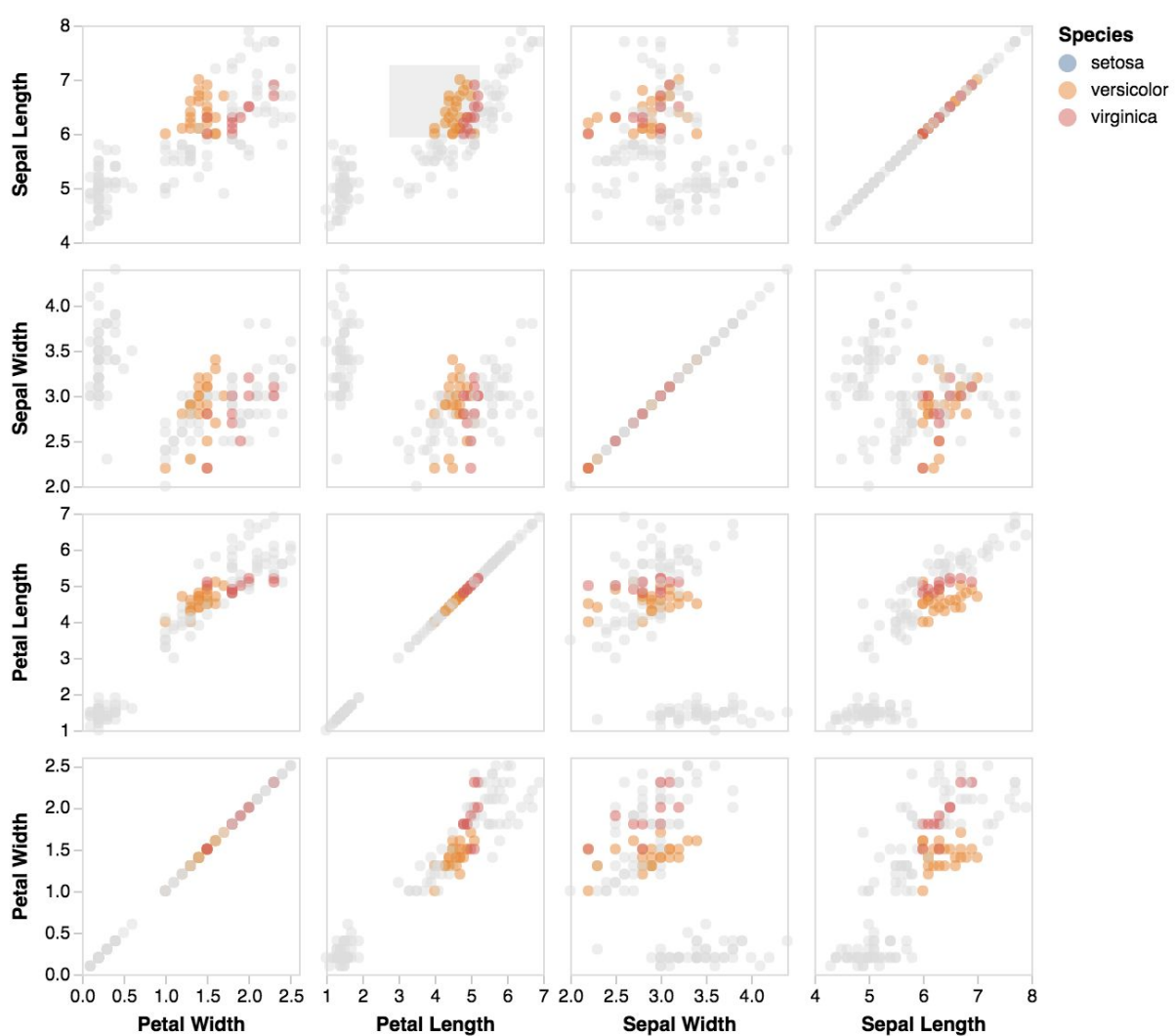


Brushing is the process of interactively selecting a subset of data items from a visual representation.

Brushing & linking cause the brush effect (highlighting, etc.) to be applied on those points in the other plots that represent the same data items.

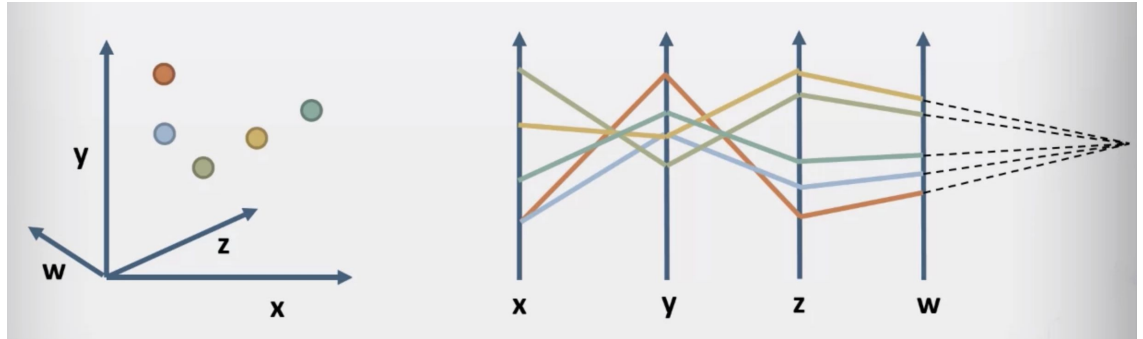
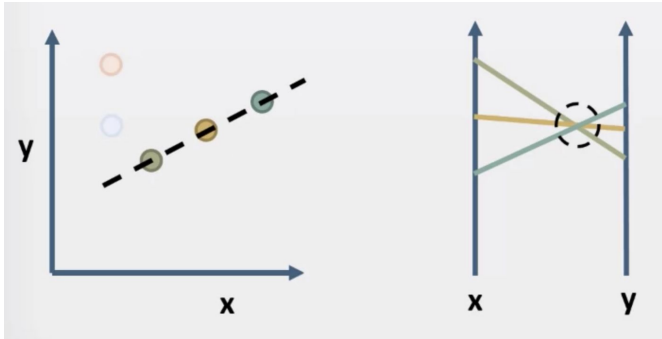
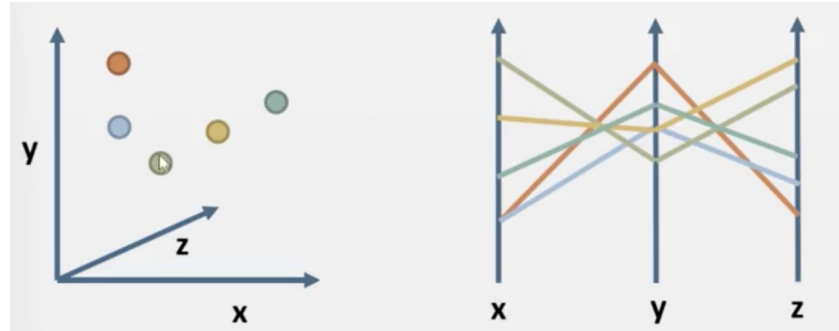
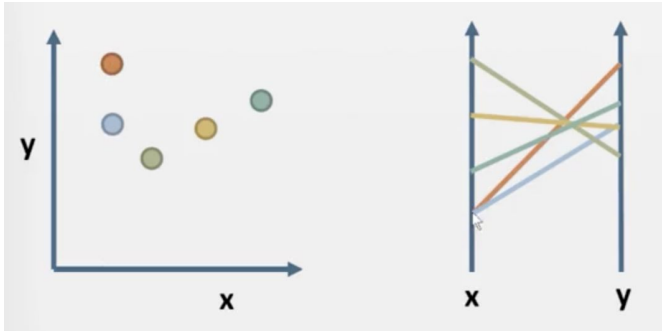
Useful for exploring relationships in multi-dimensional data.

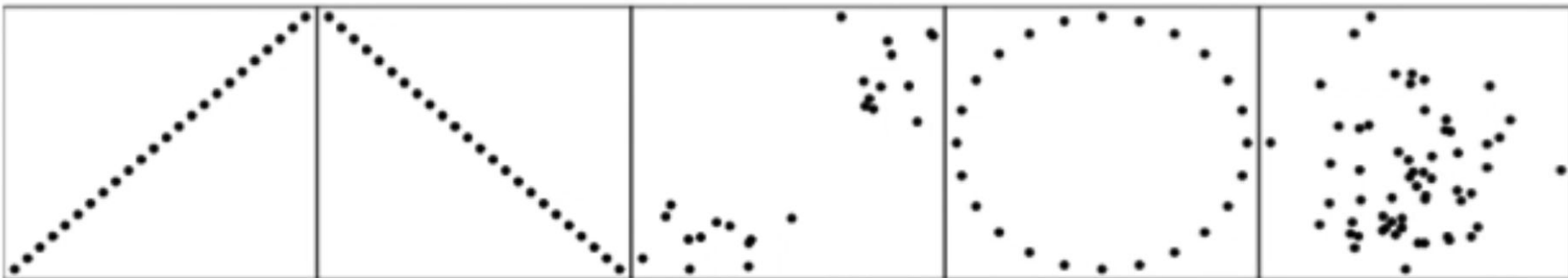
Brushing & linking scatter plots



Multi-dimensional data -- Parallel coordinates

<https://www.coursera.org/learn/datavisualization/lecture/2v40S/2-2-2-parallel-coordinates>





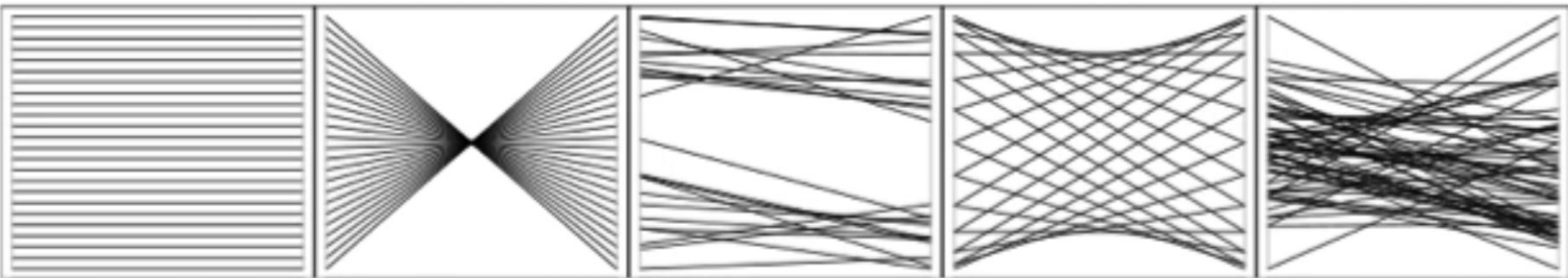
Correlation = +1

Correlation = -1

Two clusters

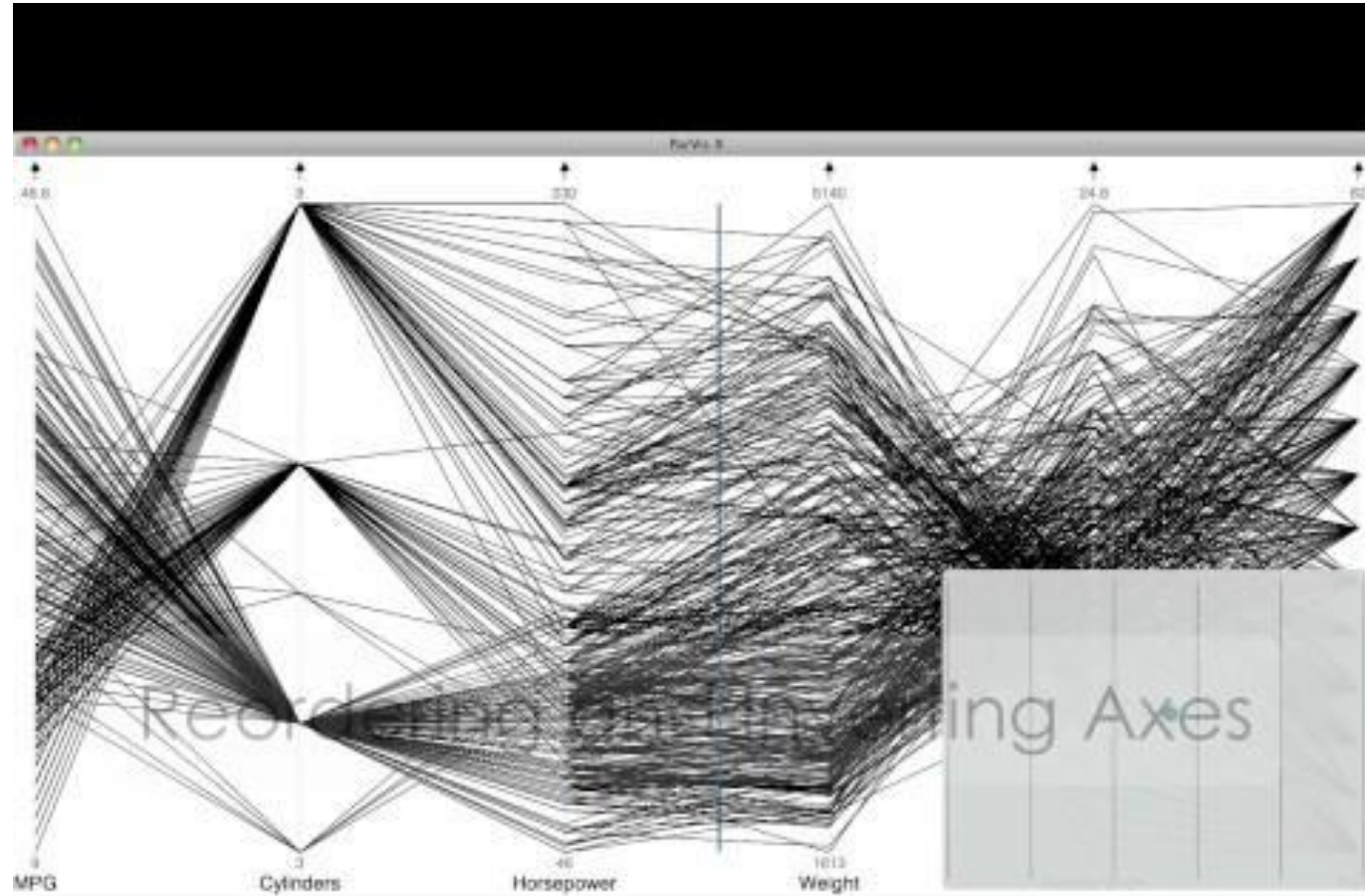
Circle

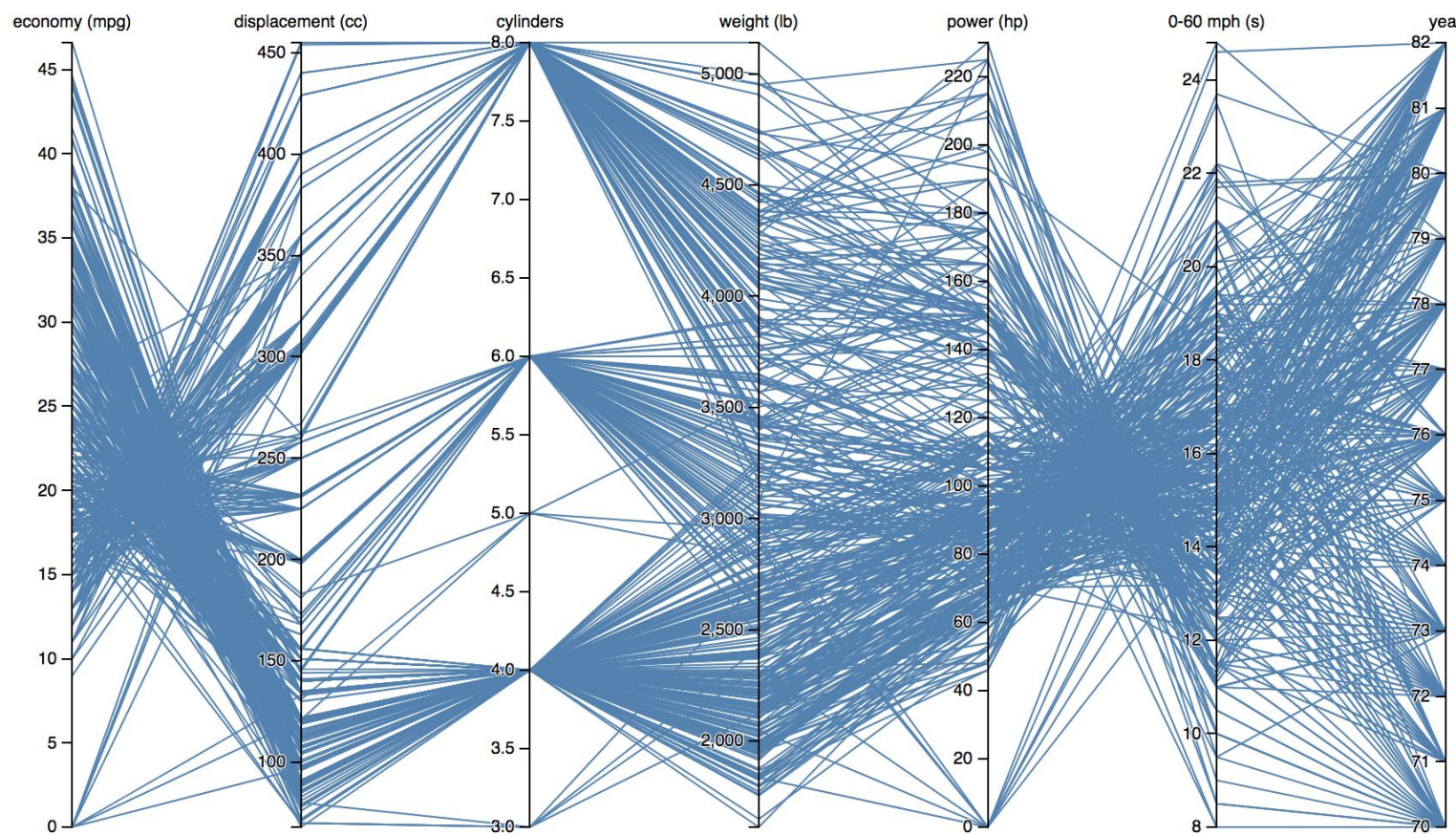
Normal distribution



Interacting with parallel coordinates

Sort an axis;
Reorder axes;
Single axis brushing;
Angular brushing.

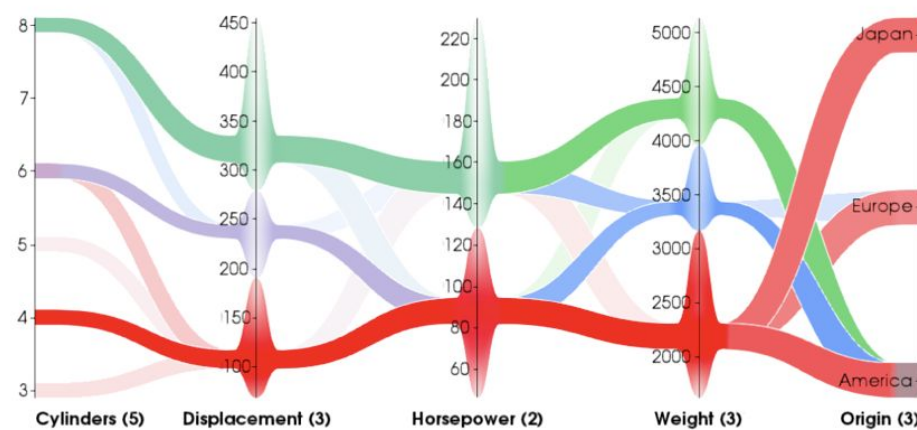
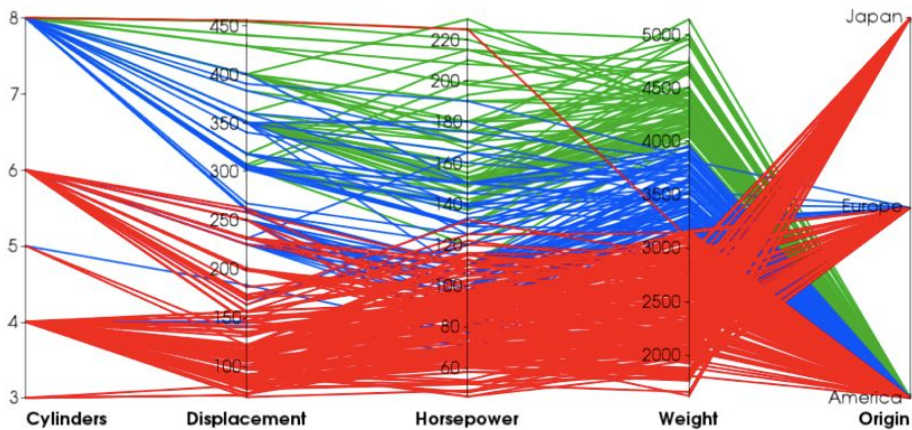




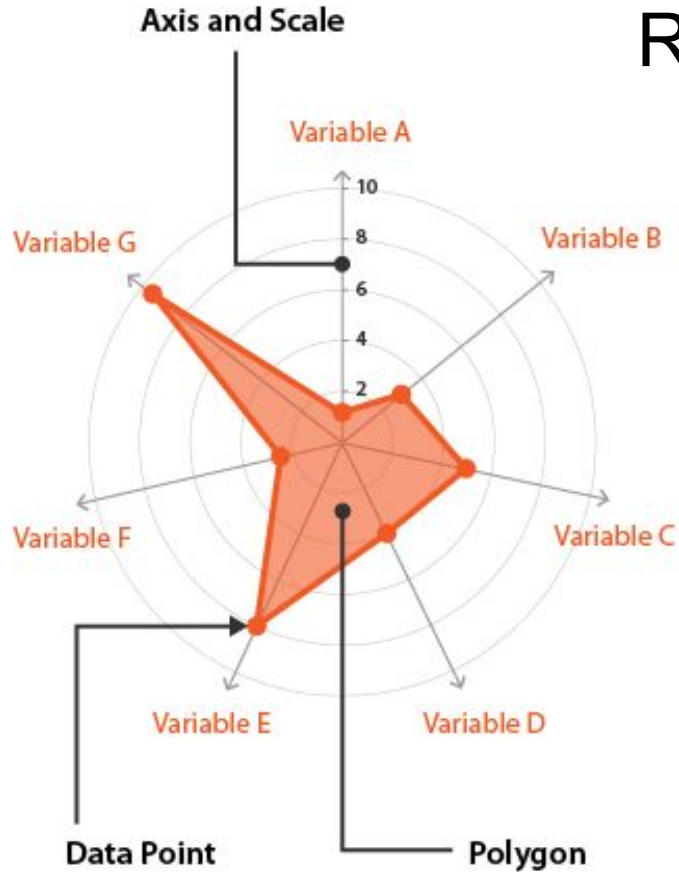
Each data value placed somewhere along the line, scaled between the minimum at the bottom and the maximum at the top.

Ordering of the axis is fundamental to draw insights.

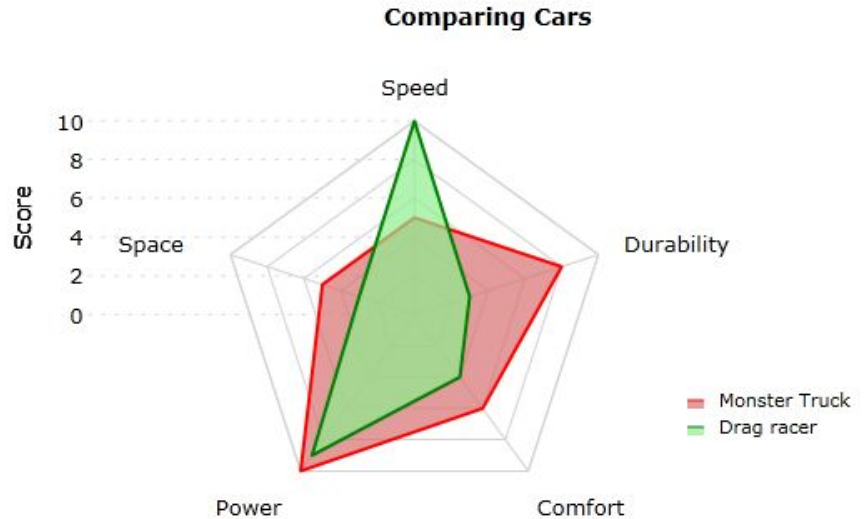
Multi-dimensional data -- Edge bundling for parallel coordinates



Radial coordinates / Radar chart

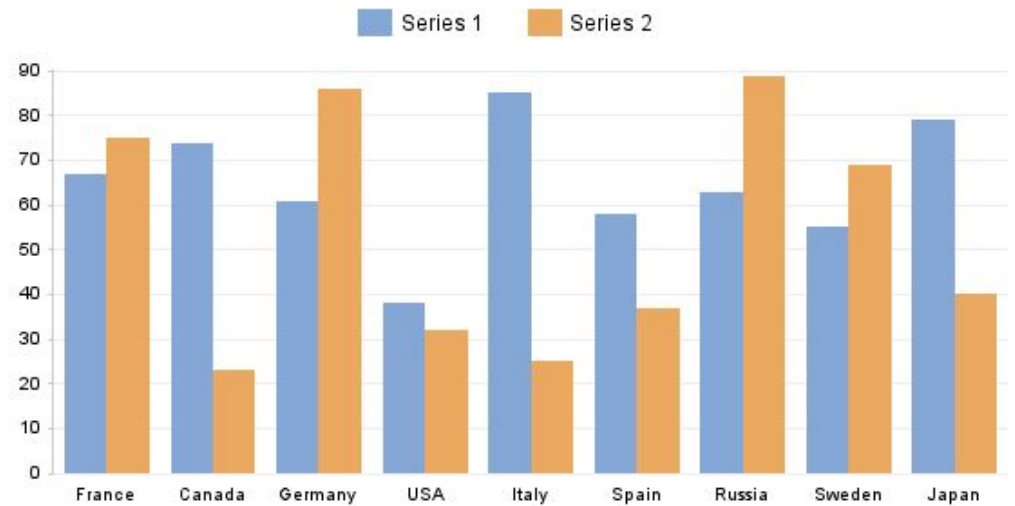
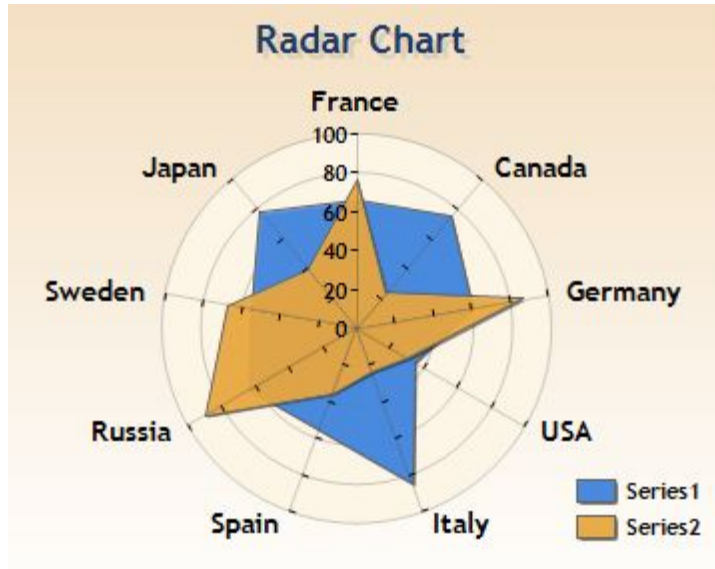


- + Useful for seeing which variables have similar values or if there are any outliers amongst each variable.
- + Visually interesting.



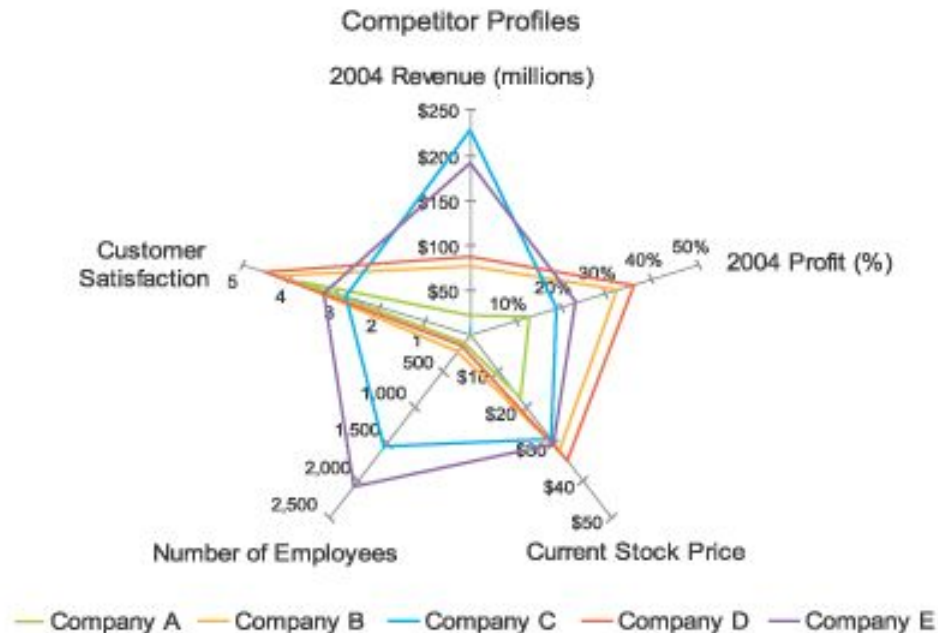
Radial coordinates / Radar chart

- Visually cluttered with too many polygons;
- Not easy to compare values along circular grids;



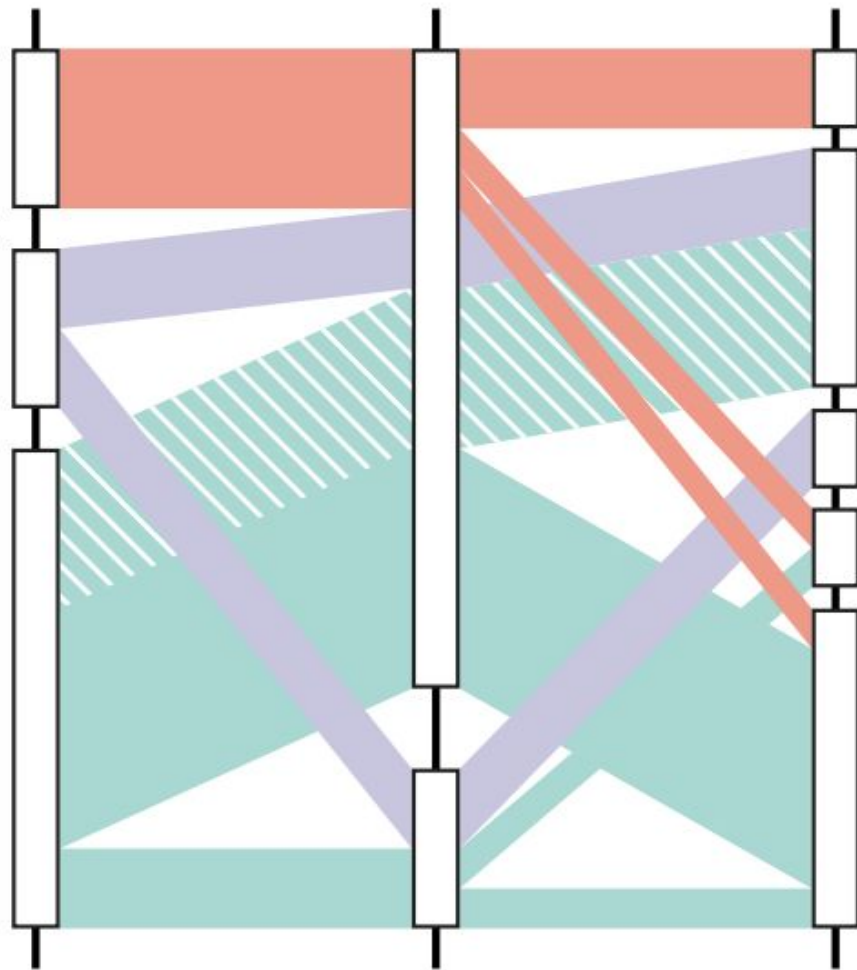
Radial coordinates / Radar chart

- When axes have different scales, values are not comparable between axes.

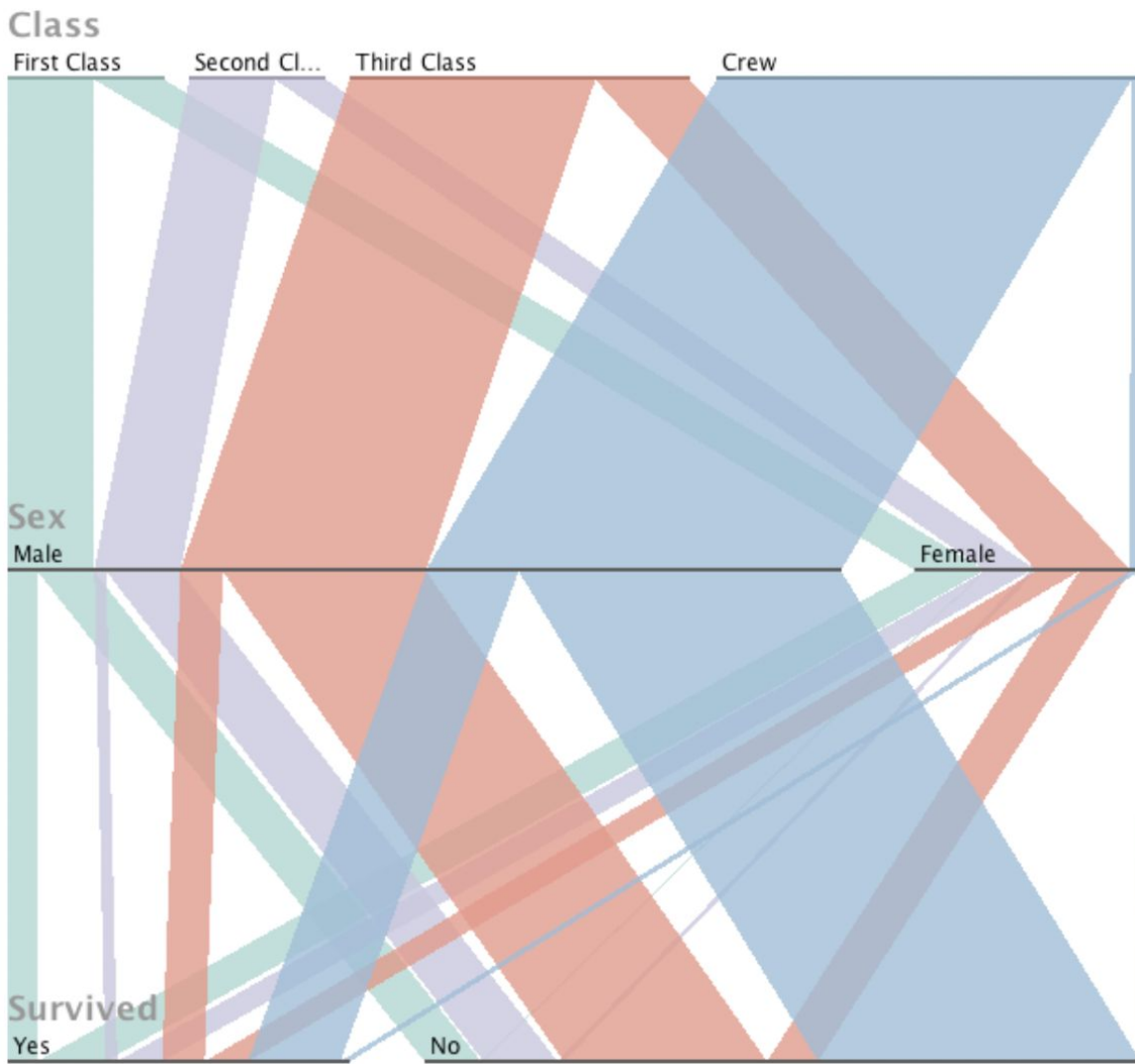


Parallel sets for categorical dimensions

Show data frequencies rather than individual data points.



Titanic Survivors

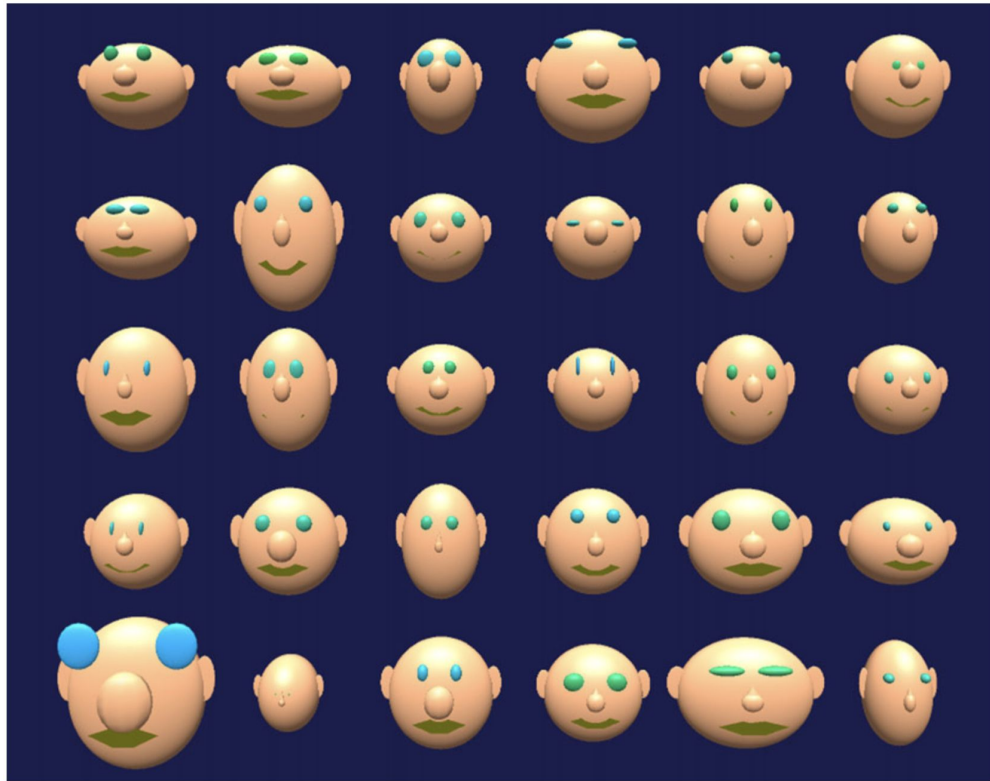


Chernoff faces

Invented by Herman Chernoff in 1973.

Encode different variables to different facial features, like the shape of the head and the size of the eye.

Assumption: object-like appearance is useful for perception.

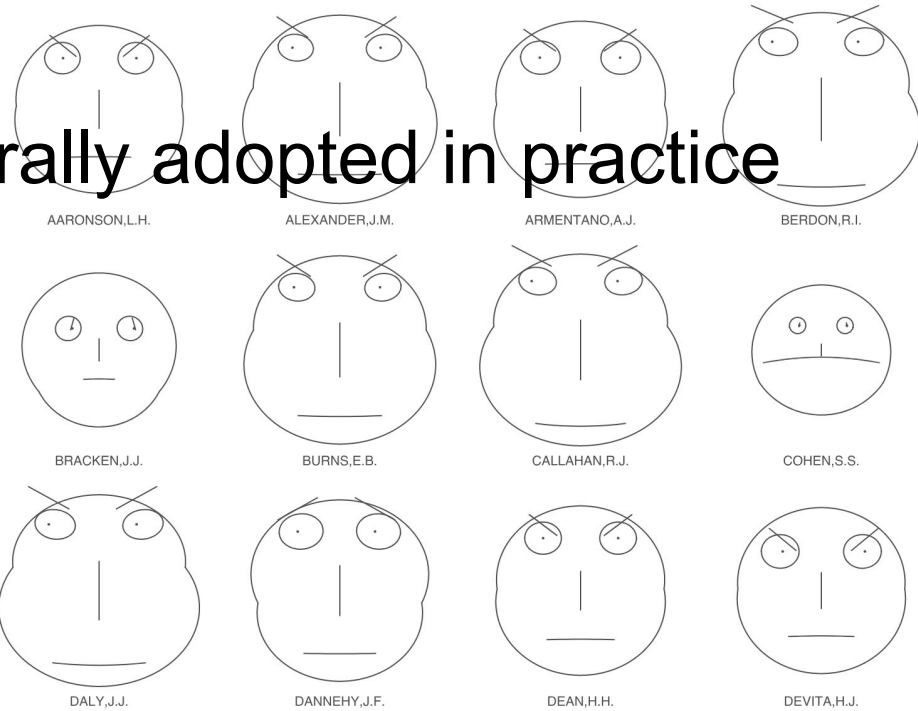


Unpredictable effects from emergent expressions.

Chernoff faces -- Not generally adopted in practice

Human differences in sensitivities to different features make the perceptual spaces likely to be non-linear.

E.g. eye size and eyebrow-slant were found to carry significant weight.



This example shows Chernoff faces for lawyers' ratings of twelve judges.

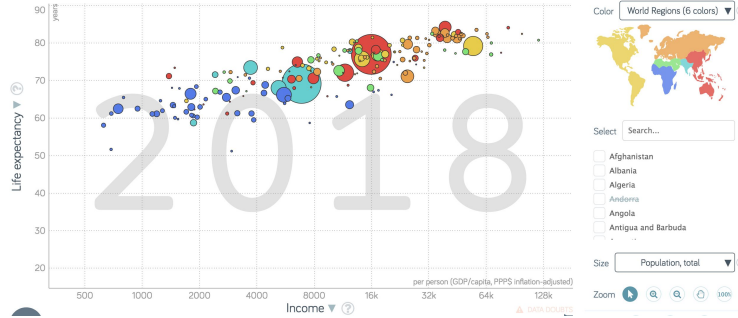
So far - 2D data

Bar chart, scatter plot, line chart, gantt chart, and table.

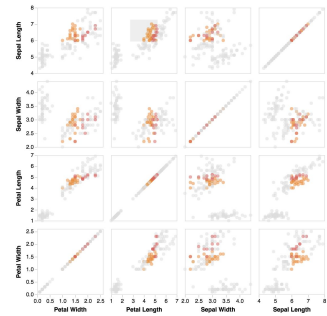
Dep.	Quantitative Continuous	Bar	Line
	Quantitative Discrete	Bar	Bar
Ind.	Quantitative Continuous	Gantt	Scatter
	Nominal or Q. Discrete	Table	Gantt
		Nominal or Q. Discrete	Quantitative Continuous
Independent			

So far - Multi-dimensional data

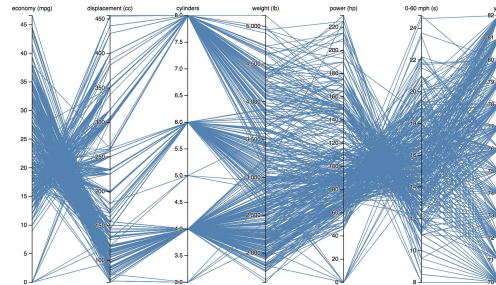
Add additional dimensions on top of 2D charts



Scatter plot matrix

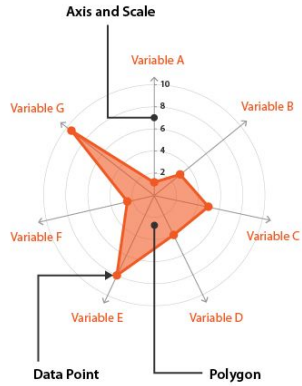


Parallel coordinates

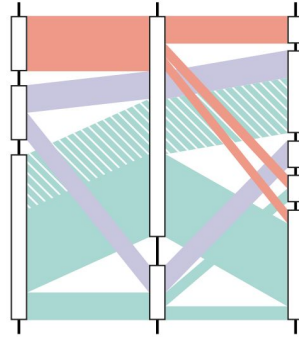


So far - Multi-dimensional data

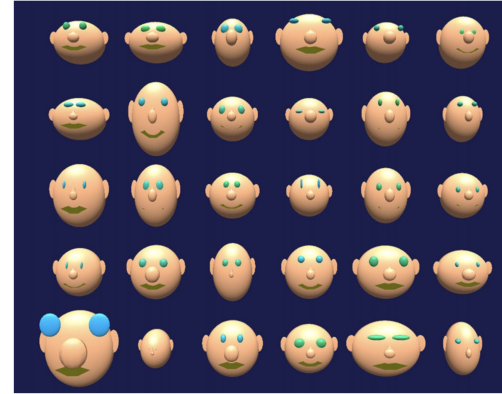
Radar chart



Parallel sets

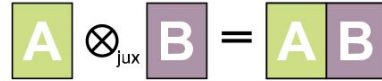


Chernoff faces

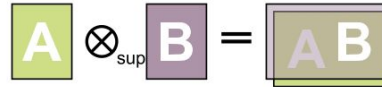


Multi-dimensional data -- Composite visualization

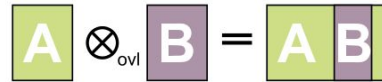
Juxtaposed views



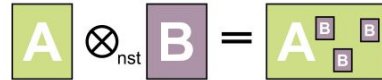
Superimposed views



Overloaded views

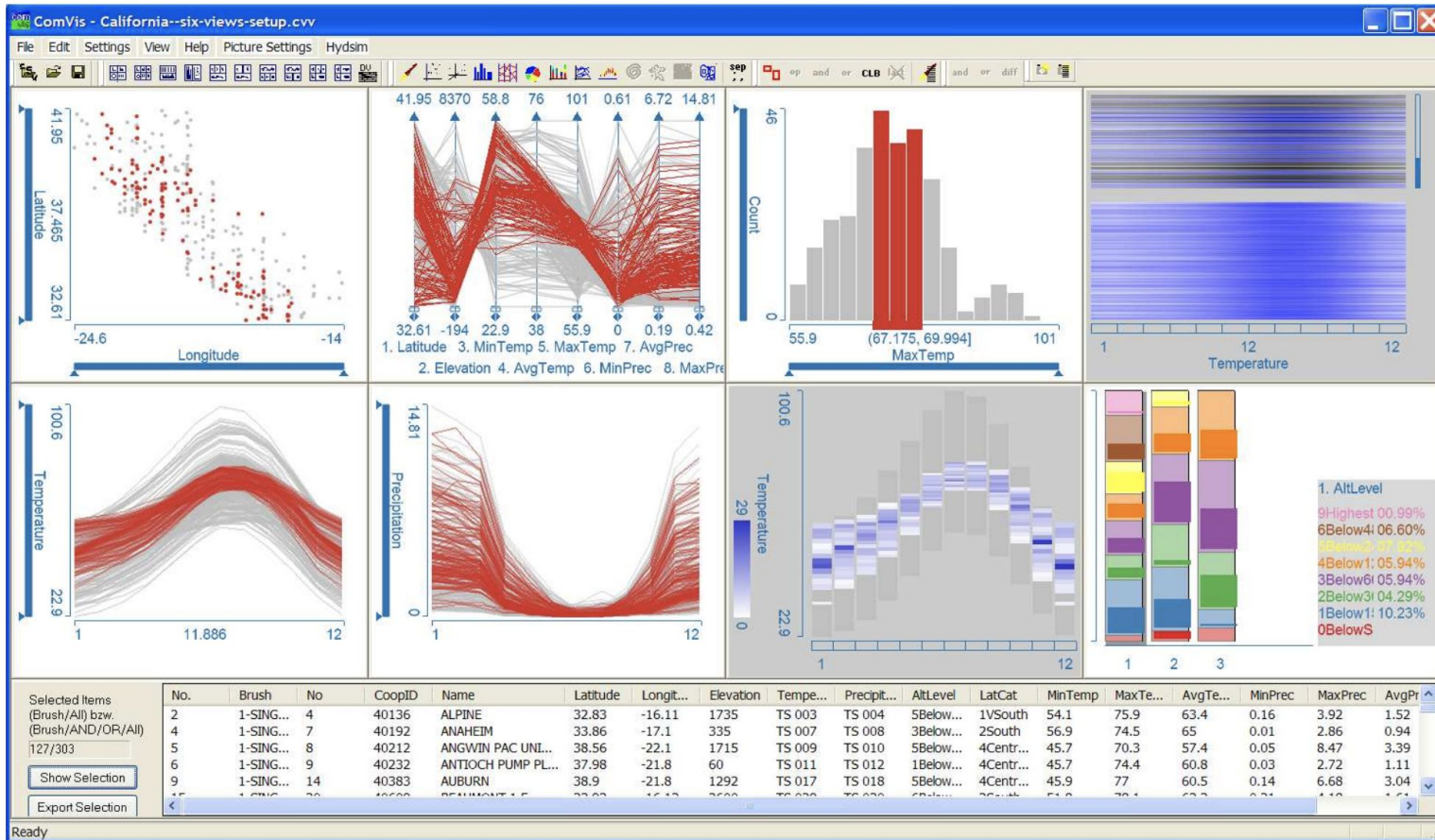


Nested views



Juxtaposed views (coordinated views) -- ComVis

Place visualizations side-by-side in one view.



Juxtaposed views (coordinated views) -- Bohemian bookshelf

Coordinate surprising aspects, like cover color and page numbers, to support serendipitous discovery.



Juxtaposed views

Implicit visual linking

Benefits

Little clutter to the resulting display.

Scalable.

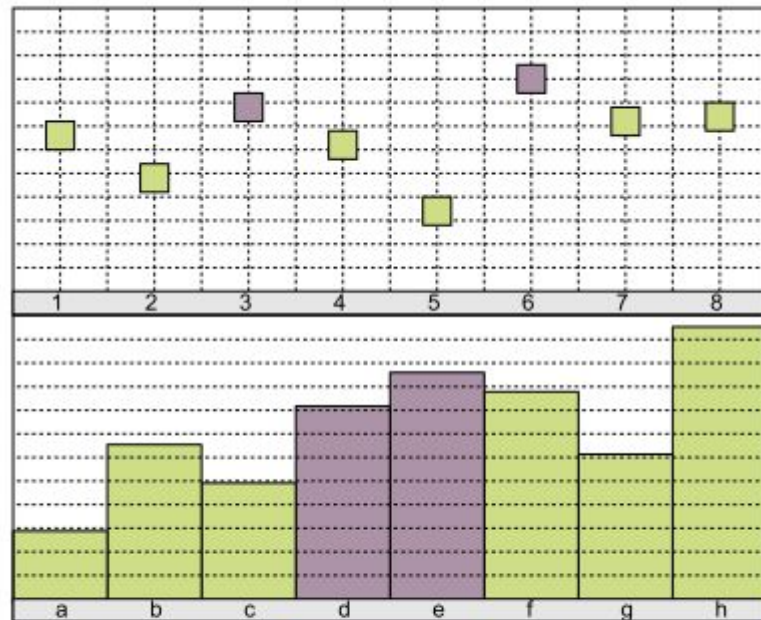
Drawback

Not easy to see implicit visual links.

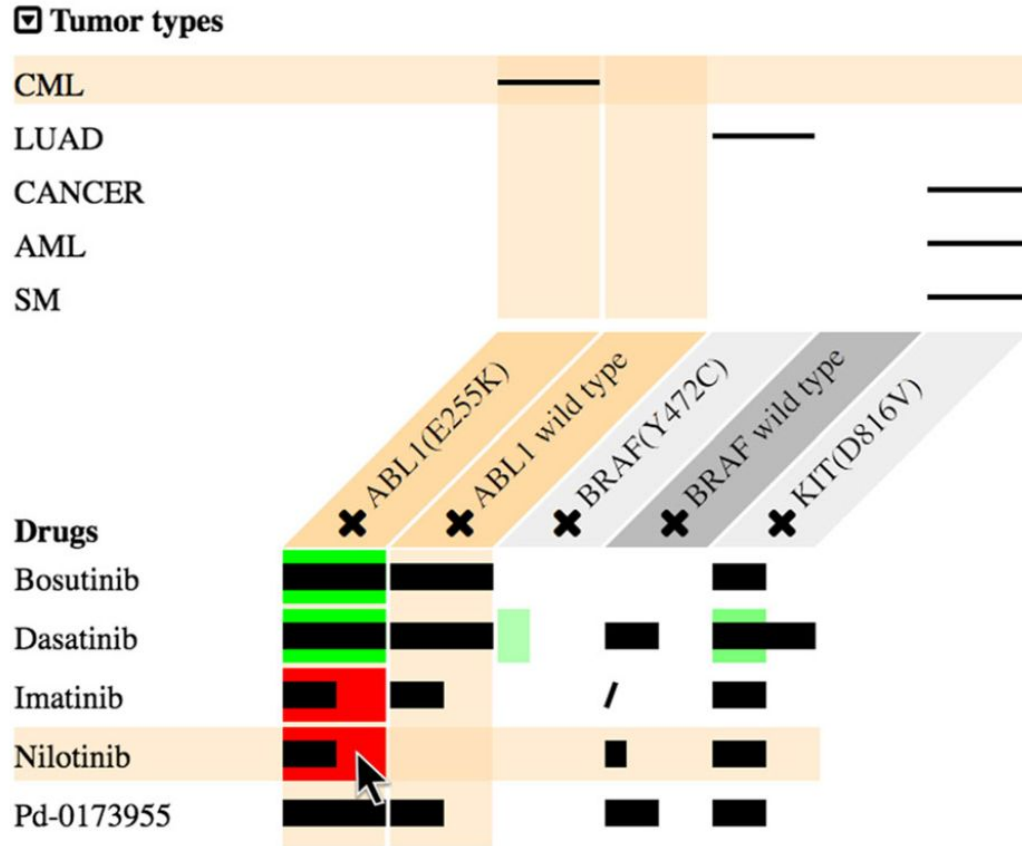
Apply for

heterogeneous datasets;

where different independent visualizations need to be combined.



Superimposed views -- Overlay two visualizations in one view.



Superimposed views

Benefits

- Direct comparison.

Drawbacks

- Visual occlusion;

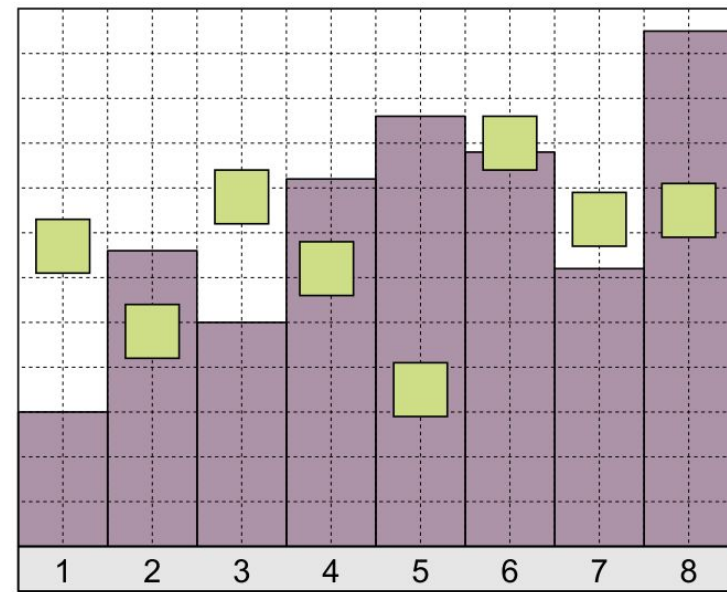
- High visual clutter;

- Multiple views need to share the same spatial mapping.

Apply for where

- comparison is common,

- the component views need to be as large as possible (potentially the entire available space).

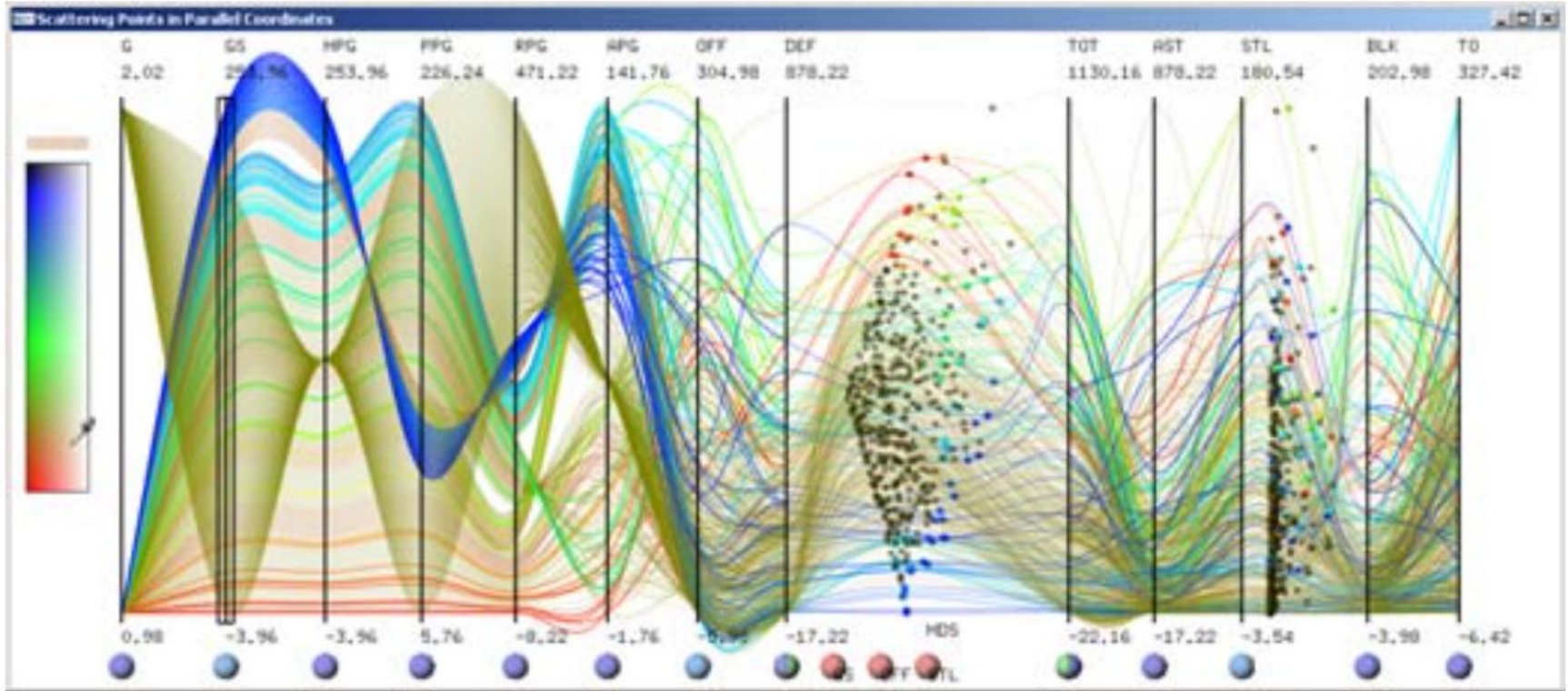


Overloaded views -- Utilize the space of one visualization for another.

Scatting points in parallel coordinates

Parallel coordinates are difficult to comprehend.

Scatter plots are more intuitive to discover correlations.



Overloaded views

Benefits

Views do not have to share the same coordinate space.

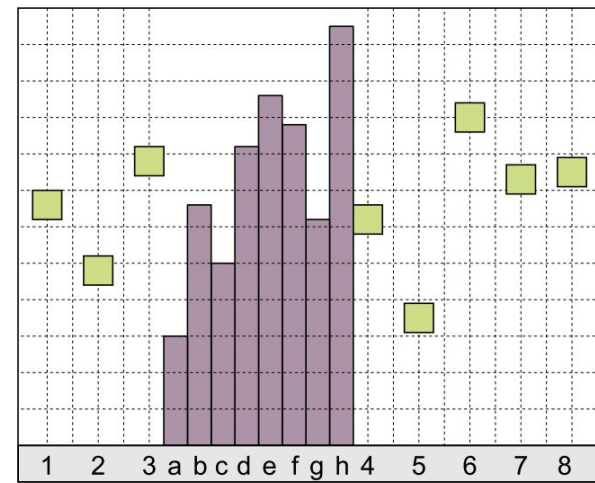
More flexibility and control over visual clutter.

Drawbacks

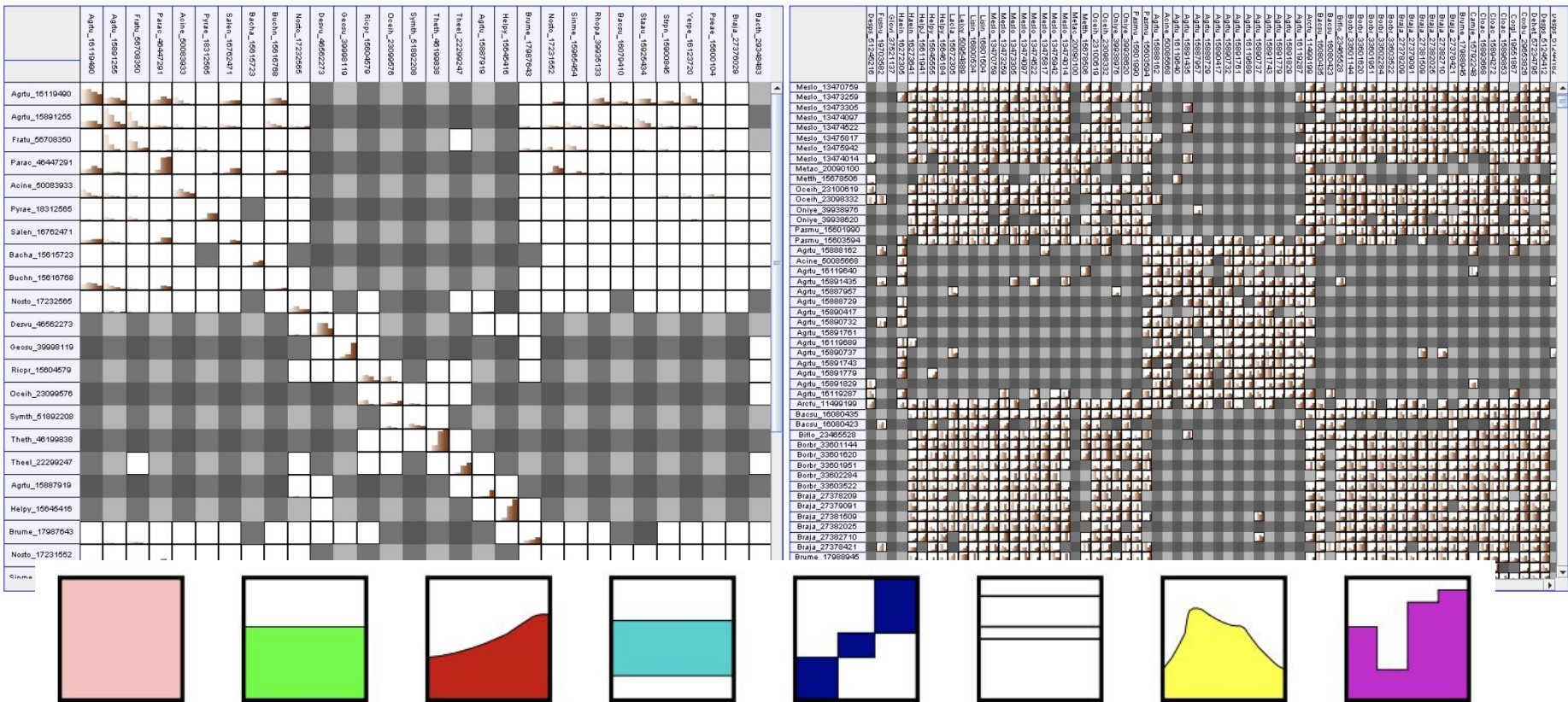
Visual clutter is increased

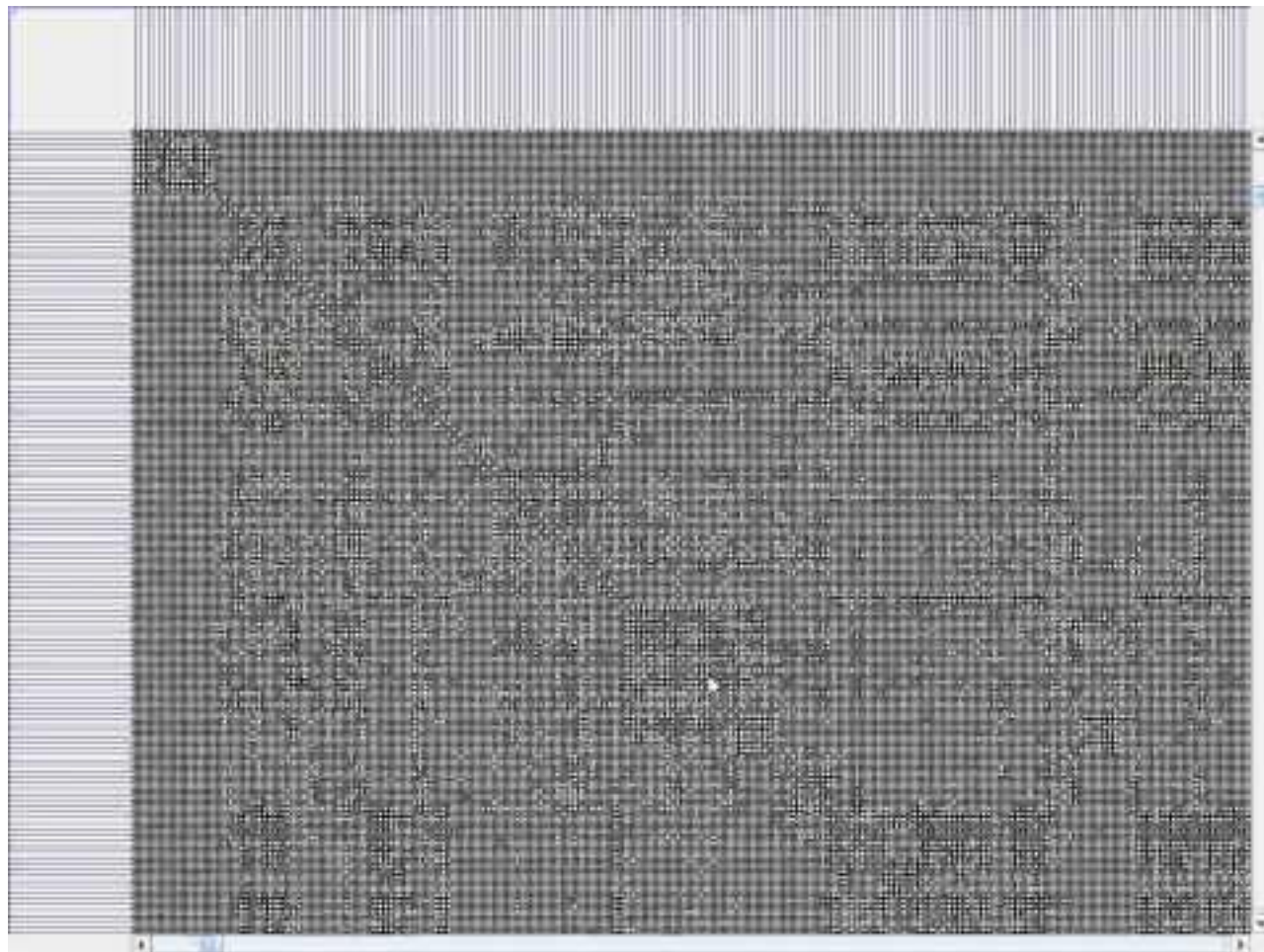
The visual design dependencies between components are significant.

Apply for situations where one visualization can be folded into another to yield a compact (and complex) result.



Nested views -- Nest the content of one visualization inside another visualization.





Nested views

Benefits

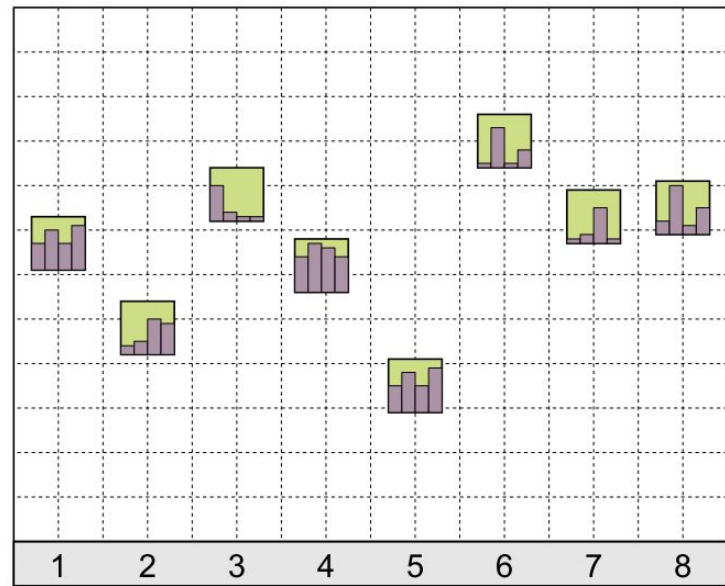
- Very compact representation;
- Easy correlation.

Drawbacks

- Limited space for the client visualizations;
- High visual clutter;
- Visual design dependencies are high.

Applications

Call for augmenting a particular visual representation with additional mapping.



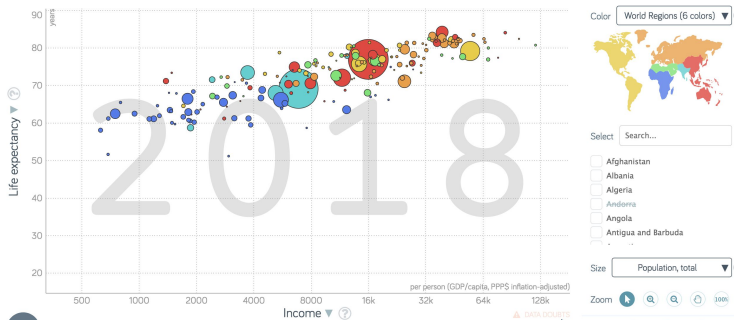
Recap - 2D data

Bar chart, scatter plot, line chart, gantt chart, and table.

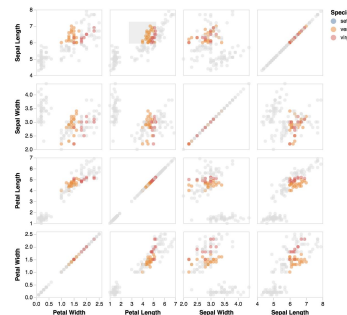
Dep.	Quantitative Continuous	Bar	Line
	Quantitative Discrete	Bar	Bar
Ind.	Quantitative Continuous	Gantt	Scatter
	Nominal or Q. Discrete	Table	Gantt
		Nominal or Q. Discrete	Quantitative Continuous
Independent			

Recap - Multi-dimensional data

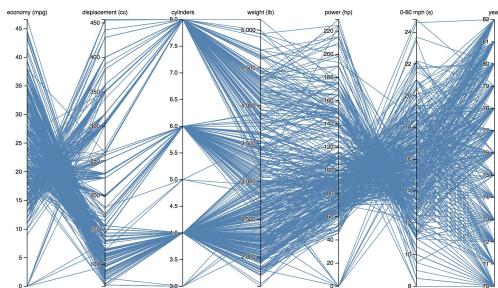
Add additional dimensions on top of 2D charts



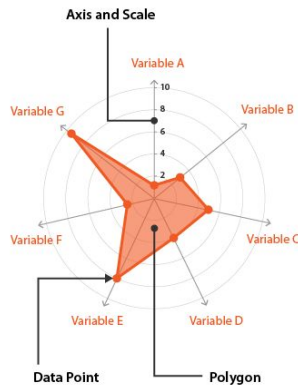
Scatter plot matrix



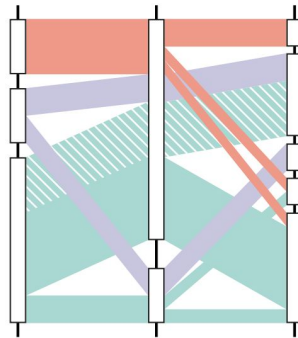
Parallel coordinates



Radar chart

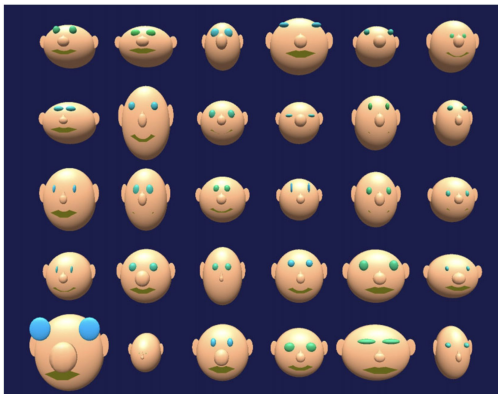


Parallel sets



Recap - Multi-dimensional data

Chernoff faces



Composite views

Juxtaposed views

$$A \otimes_{\text{jux}} B = \begin{array}{|c|c|} \hline A & B \\ \hline \end{array}$$

Superimposed views

$$A \otimes_{\text{sup}} B = \begin{array}{|c|c|} \hline A & B \\ \hline \end{array}$$

Overloaded views

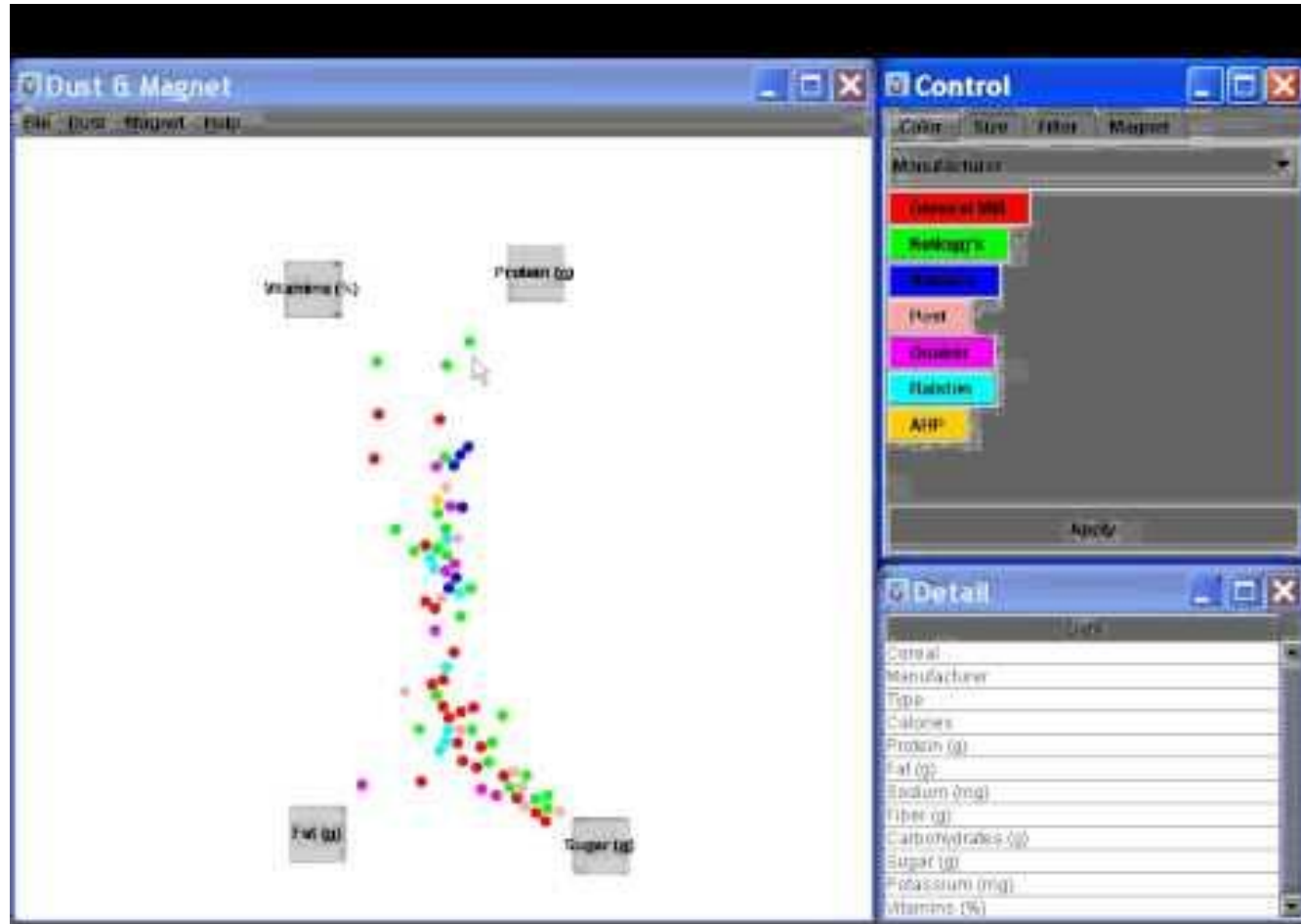
$$A \otimes_{\text{ovl}} B = \begin{array}{|c|c|} \hline A & B \\ \hline \end{array}$$

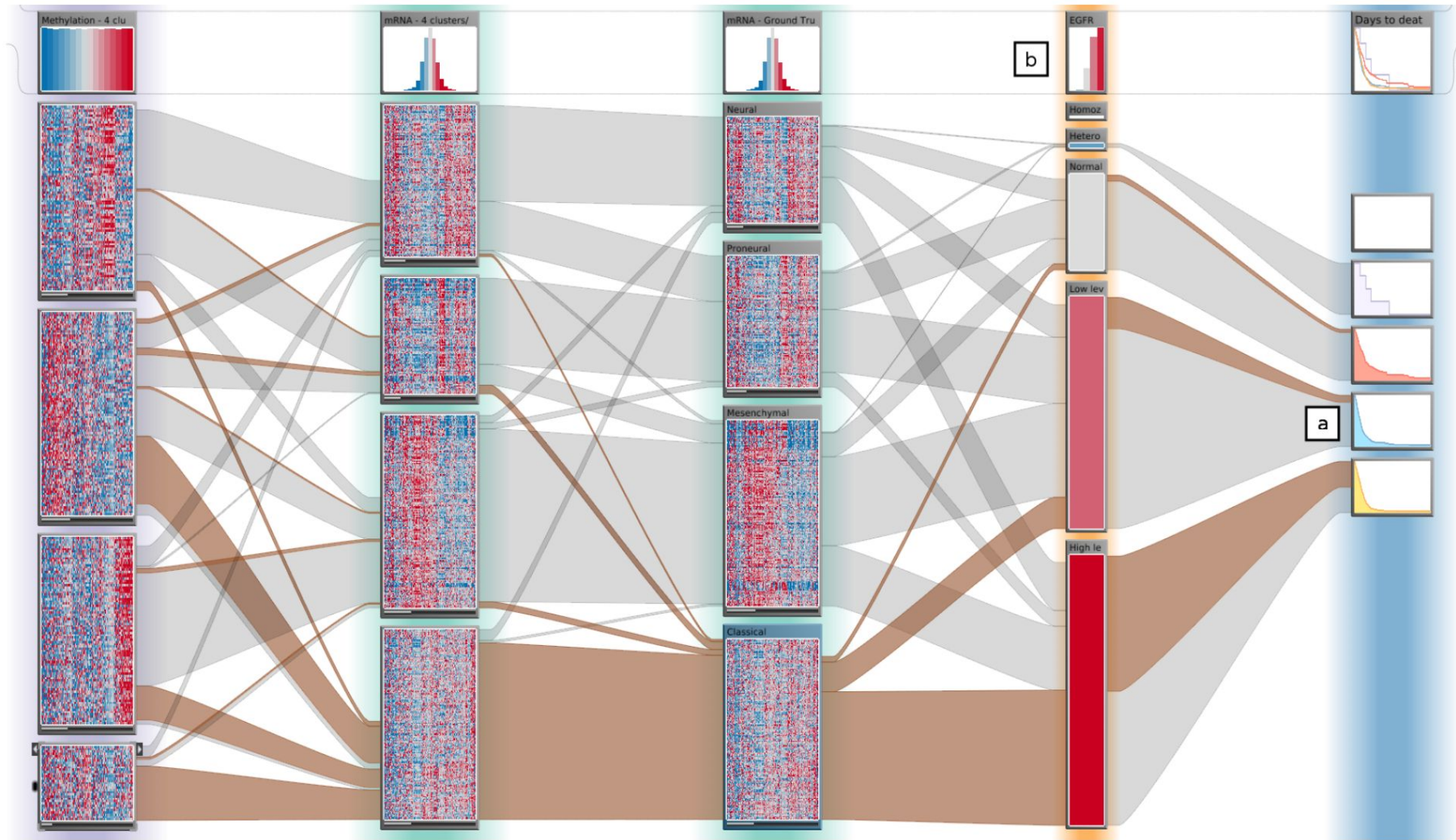
Nested views

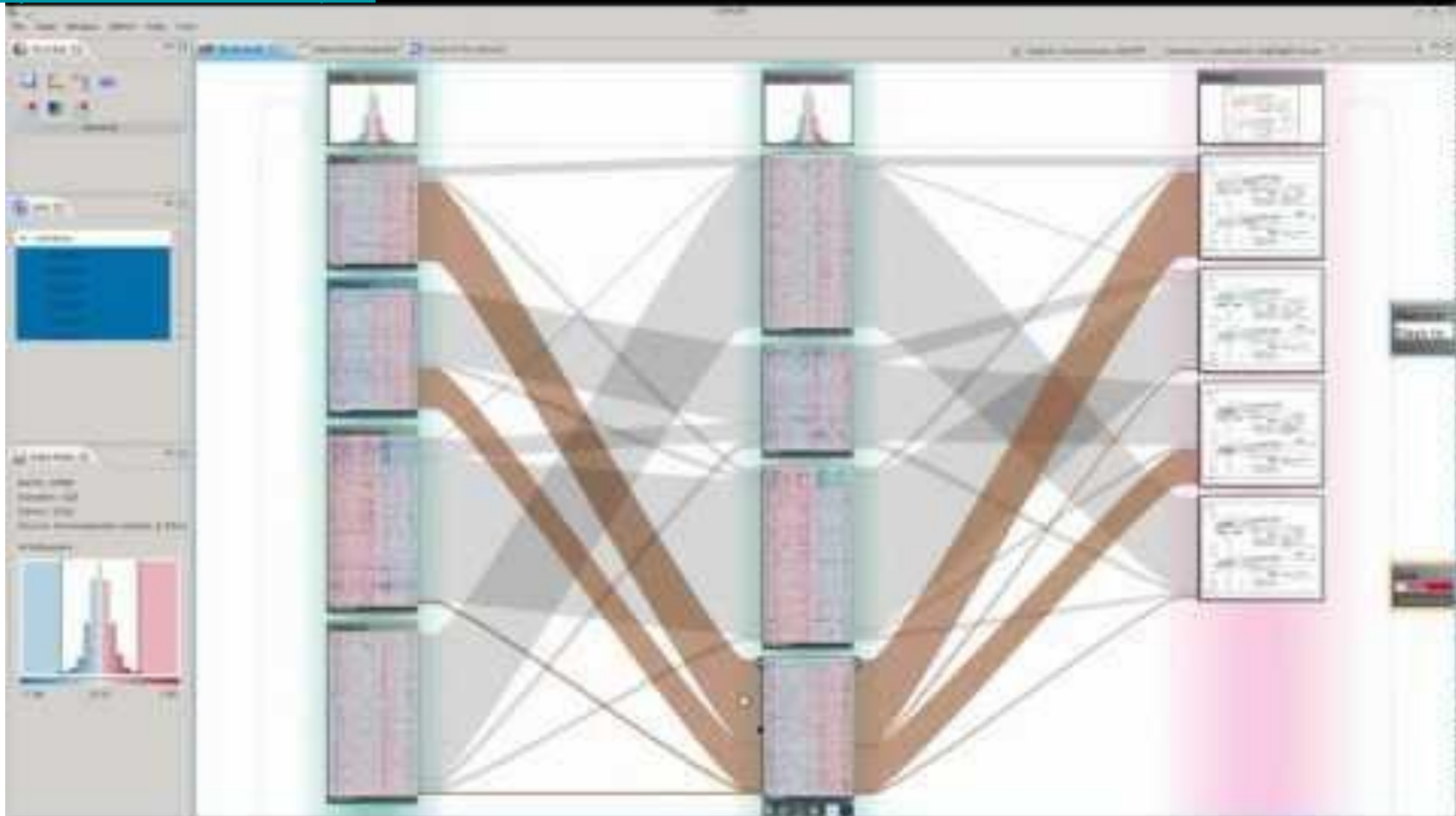
$$A \otimes_{\text{nst}} B = \begin{array}{|c|c|} \hline A & B \\ \hline \end{array}$$

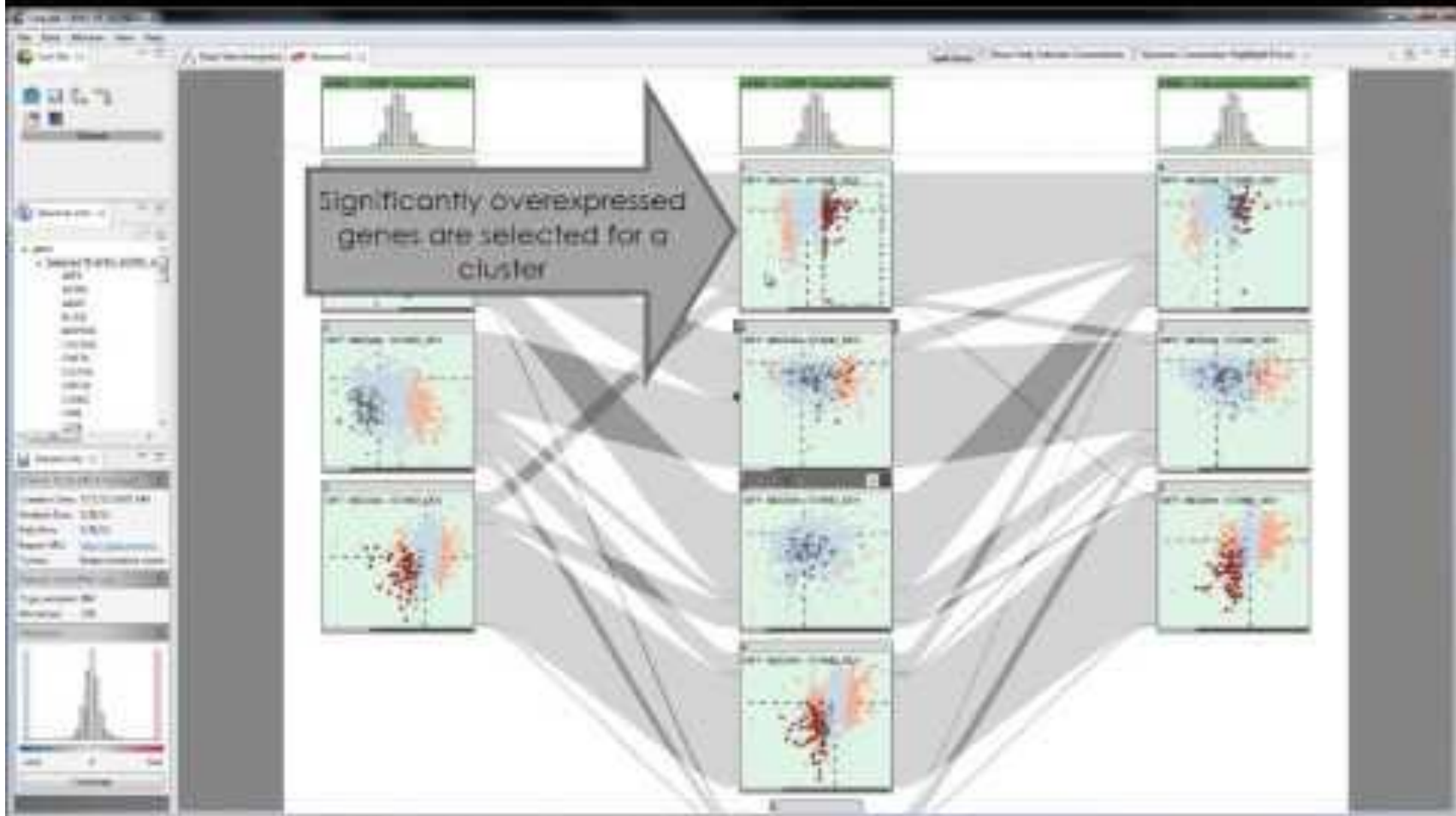
Applications of multi-dimensional data visualizations

Magnet metaphor

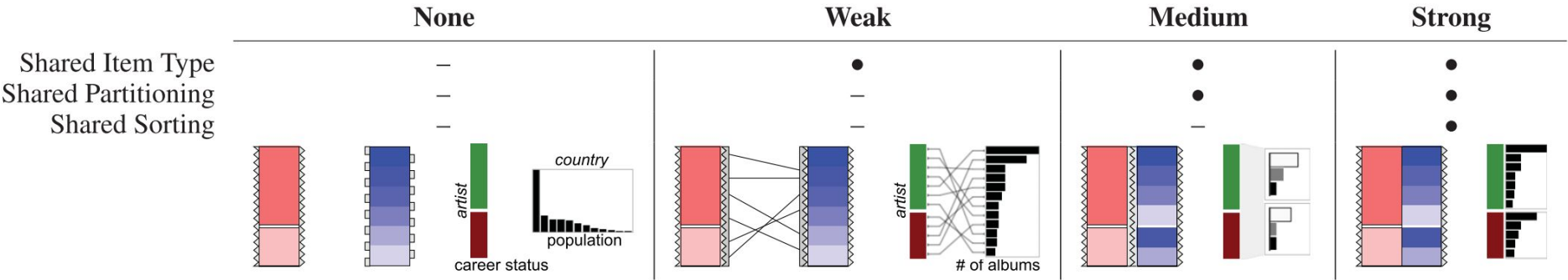
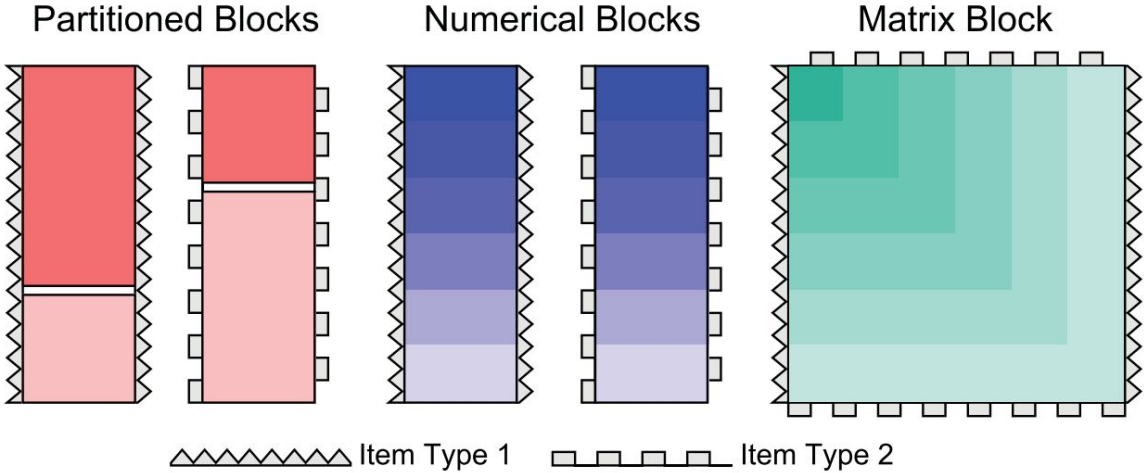




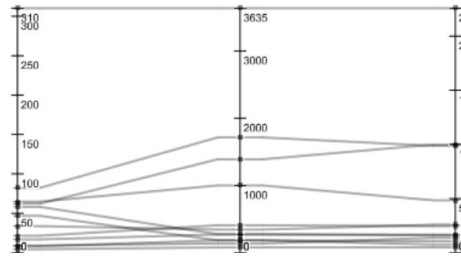
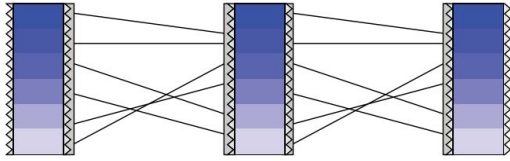




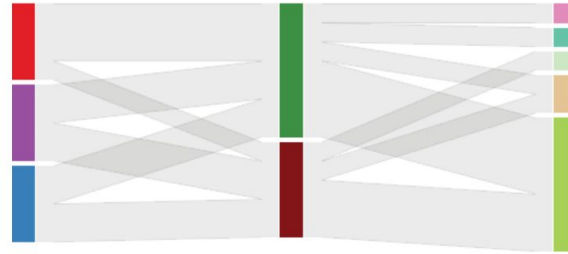
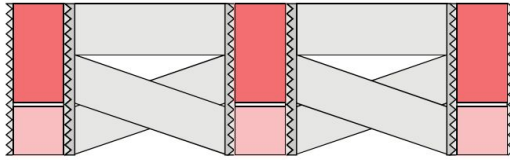
Domino: Relations across multiple tabular datasets.



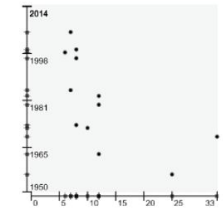
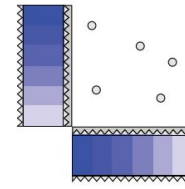
(a) Parallel Coordinate Plot [14]



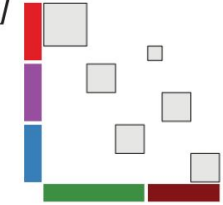
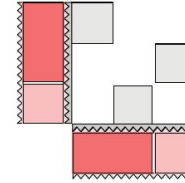
(c) Parallel Sets [18]



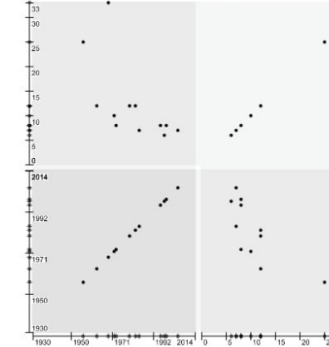
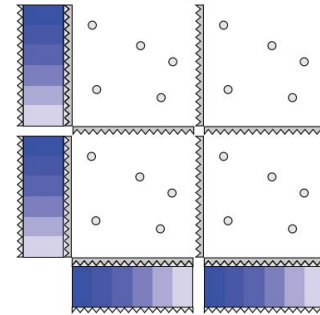
(b) Scatterplot



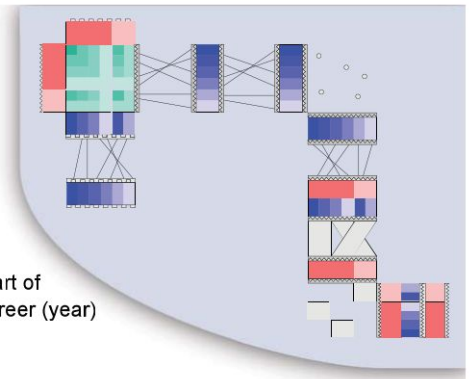
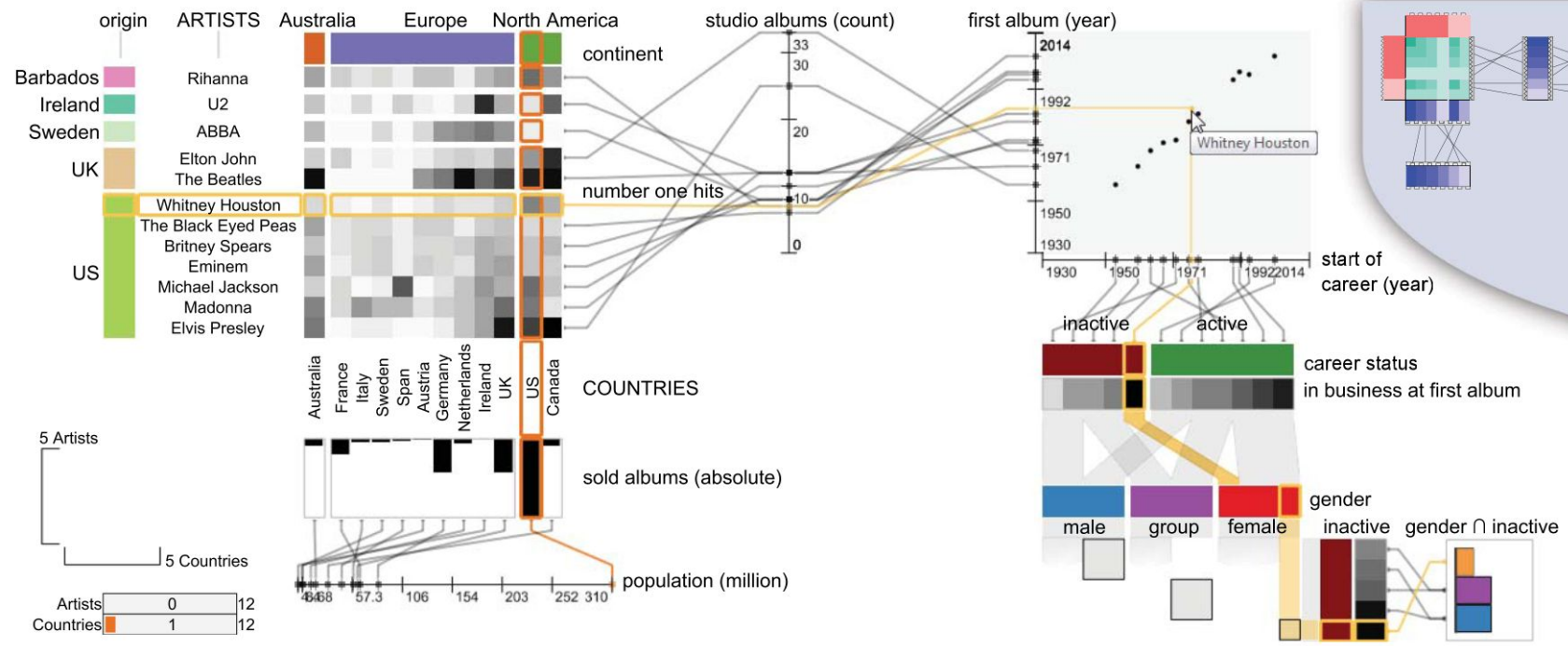
(d) Mosaic Plot [11]

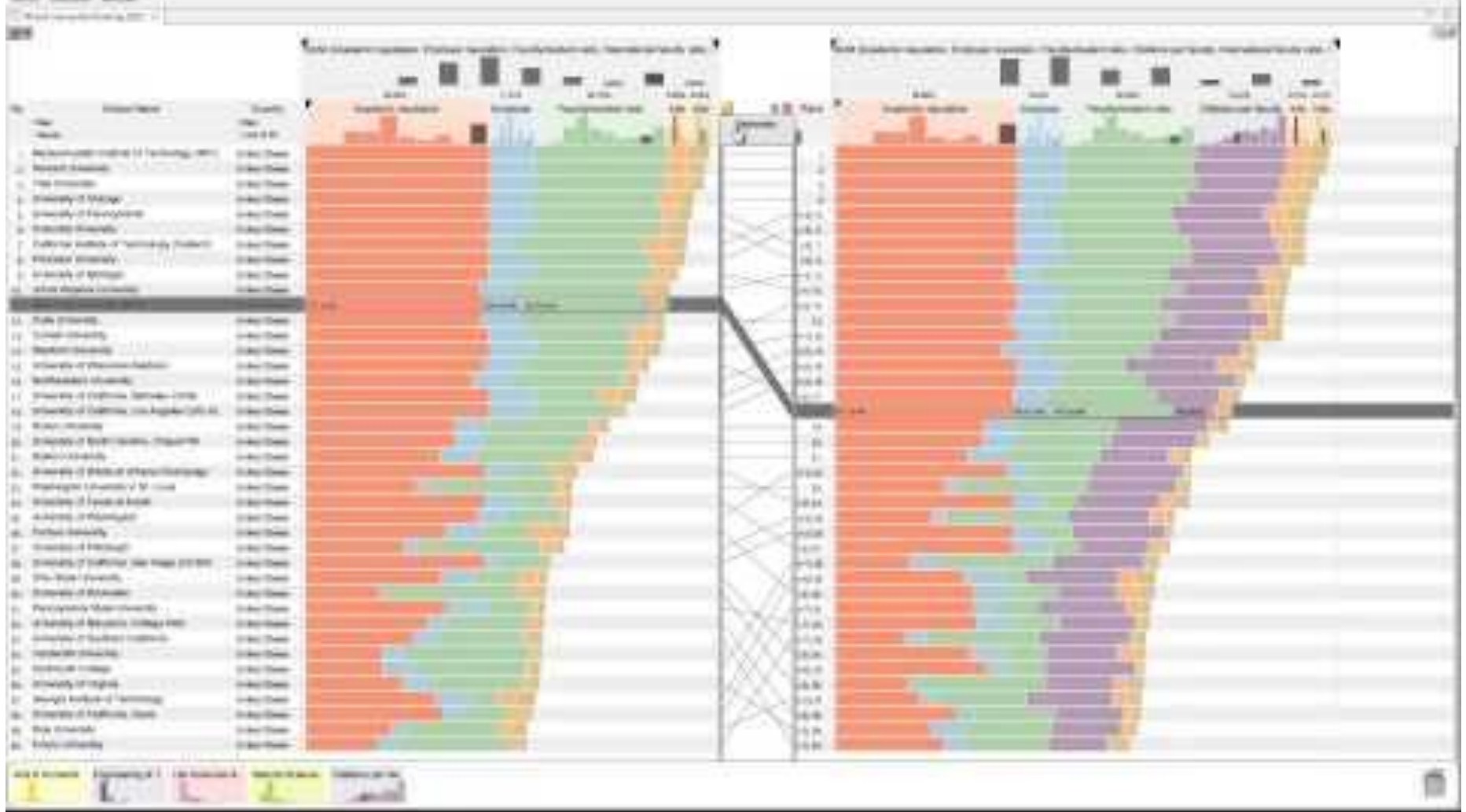


(f) Scatterplot Matrix (SPLOM) [4]



Domino: Relations across multiple tabular datasets





References

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